

# APPENDIX **A**

## *Thermophysical Properties of Matter*<sup>1</sup>

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<sup>1</sup> The convention used to present numerical values of the properties is illustrated by this example:

| $T$<br>(K) | $\nu \cdot 10^7$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) |
|------------|-----------------------------------------|-----------------------------|
| 300        | 0.349                                   | 521                         |

where  $\nu = 0.349 \times 10^{-7}$  m<sup>2</sup>/s and  $k = 521 \times 10^{-3} = 0.521$  W/m · K at 300 K.

TABLE A.1 Thermophysical Properties of Selected Metallic Solids<sup>a</sup>

| Composition                                     | Melting Point (K) | Properties at 300 K  |            |           |                     | Properties at Various Temperatures (K) |      |      |      |      |      |      |      |      |      |
|-------------------------------------------------|-------------------|----------------------|------------|-----------|---------------------|----------------------------------------|------|------|------|------|------|------|------|------|------|
|                                                 |                   | $\rho$               | $c_p$      | $k$       | $\alpha \cdot 10^6$ | $k$ (W/m · K)/ $c_p$ (J/kg · K)        |      |      |      |      |      |      |      |      |      |
|                                                 |                   | (kg/m <sup>3</sup> ) | (J/kg · K) | (W/m · K) | (m <sup>2</sup> /s) | 100                                    | 200  | 400  | 600  | 800  | 1000 | 1200 | 1500 | 2000 | 2500 |
| Aluminum<br>Pure                                | 933               | 2702                 | 903        | 237       | 97.1                | 302                                    | 237  | 240  | 231  | 218  |      |      |      |      |      |
| Alloy 2024-T6<br>(4.5% Cu, 1.5% Mg,<br>0.6% Mn) | 775               | 2770                 | 875        | 177       | 73.0                | 482                                    | 798  | 949  | 1033 | 1146 |      |      |      |      |      |
| Alloy 195, Cast<br>(4.5% Cu)                    |                   | 2790                 | 883        | 168       | 68.2                | 473                                    | 787  | 925  | 1042 |      |      |      |      |      |      |
| Beryllium                                       | 1550              | 1850                 | 1825       | 200       | 59.2                | 990                                    | 301  | 161  | 126  | 106  | 90.8 | 78.7 |      |      |      |
|                                                 |                   |                      |            |           |                     | 203                                    | 1114 | 2191 | 2604 | 2823 | 3018 | 3227 | 3519 |      |      |
| Bismuth                                         | 545               | 9780                 | 122        | 7.86      | 6.59                | 16.5                                   | 9.69 | 7.04 |      |      |      |      |      |      |      |
|                                                 |                   |                      |            |           |                     | 112                                    | 120  | 127  |      |      |      |      |      |      |      |
| Boron                                           | 2573              | 2500                 | 1107       | 27.0      | 9.76                | 190                                    | 55.5 | 16.8 | 10.6 | 9.60 | 9.85 |      |      |      |      |
|                                                 |                   |                      |            |           |                     | 128                                    | 600  | 1463 | 1892 | 2160 | 2338 |      |      |      |      |
| Cadmium                                         | 594               | 8650                 | 231        | 96.8      | 48.4                | 203                                    | 99.3 | 94.7 |      |      |      |      |      |      |      |
|                                                 |                   |                      |            |           |                     | 198                                    | 222  | 242  |      |      |      |      |      |      |      |
| Chromium                                        | 2118              | 7160                 | 449        | 93.7      | 29.1                | 159                                    | 111  | 90.9 | 80.7 | 71.3 | 65.4 | 61.9 | 57.2 | 49.4 |      |
|                                                 |                   |                      |            |           |                     | 192                                    | 384  | 484  | 542  | 581  | 616  | 682  | 779  | 937  |      |
| Cobalt                                          | 1769              | 8862                 | 421        | 99.2      | 26.6                | 167                                    | 122  | 85.4 | 67.4 | 58.2 | 52.1 | 49.3 | 42.5 |      |      |
|                                                 |                   |                      |            |           |                     | 236                                    | 379  | 450  | 503  | 550  | 628  | 733  | 674  |      |      |
| Copper<br>Pure                                  | 1358              | 8933                 | 385        | 401       | 117                 | 482                                    | 413  | 393  | 379  | 366  | 352  | 339  |      |      |      |
|                                                 |                   |                      |            |           |                     | 252                                    | 356  | 397  | 417  | 433  | 451  | 480  |      |      |      |
| Commercial bronze<br>(90% Cu, 10% Al)           | 1293              | 8800                 | 420        | 52        | 14                  |                                        | 42   | 52   | 59   |      |      |      |      |      |      |
| Phosphor gear bronze<br>(89% Cu, 11% Sn)        | 1104              | 8780                 | 355        | 54        | 17                  |                                        | 785  | 460  | 545  |      |      |      |      |      |      |
| Cartridge brass<br>(70% Cu, 30% Zn)             | 1188              | 8530                 | 380        | 110       | 33.9                | 75                                     | 95   | 137  | 149  |      |      |      |      |      |      |
| Constantan<br>(55% Cu, 45% Ni)                  | 1493              | 8920                 | 384        | 23        | 6.71                | 17                                     | 19   | 395  | 425  |      |      |      |      |      |      |
|                                                 |                   |                      |            |           |                     | 237                                    | 362  |      |      |      |      |      |      |      |      |
| Germanium                                       | 1211              | 5360                 | 322        | 59.9      | 34.7                | 232                                    | 96.8 | 43.2 | 27.3 | 19.8 | 17.4 | 17.4 |      |      |      |
|                                                 |                   |                      |            |           |                     | 190                                    | 290  | 337  | 348  | 357  | 375  | 395  |      |      |      |

|                                       |      |       |     |      |      |      |      |      |      |      |      |      |
|---------------------------------------|------|-------|-----|------|------|------|------|------|------|------|------|------|
| Gold                                  | 1336 | 19300 | 129 | 317  | 127  | 327  | 323  | 311  | 298  | 284  | 270  | 255  |
| Iridium                               | 2720 | 22500 | 130 | 147  | 50.3 | 172  | 153  | 144  | 138  | 132  | 126  | 120  |
| Iron                                  |      |       |     |      |      | 90   | 122  | 133  | 138  | 144  | 153  | 161  |
| Pure                                  | 1810 | 7870  | 447 | 80.2 | 23.1 | 134  | 94.0 | 69.5 | 54.7 | 43.3 | 32.8 | 28.3 |
| Armco                                 |      |       |     |      |      | 216  | 384  | 490  | 574  | 680  | 975  | 609  |
| (99.75% pure)                         | 7870 | 7870  | 447 | 72.7 | 20.7 | 95.6 | 80.6 | 65.7 | 53.1 | 42.2 | 32.3 | 28.7 |
|                                       |      |       |     |      |      | 215  | 384  | 490  | 574  | 680  | 975  | 609  |
| Carbon steels                         |      |       |     |      |      |      |      |      |      |      |      |      |
| Plain carbon                          |      |       |     |      |      |      |      |      |      |      |      |      |
| (Mn $\leq$ 1%,                        |      |       |     |      |      |      |      |      |      |      |      |      |
| Si $\leq$ 0.1%)                       |      |       |     |      |      |      |      |      |      |      |      |      |
| AISI 1010                             |      |       |     |      |      |      |      |      |      |      |      |      |
| Carbon-silicon                        |      |       |     |      |      |      |      |      |      |      |      |      |
| (Mn $\leq$ 1%,                        |      |       |     |      |      |      |      |      |      |      |      |      |
| 0.1% < Si $\leq$ 0.6%)                |      |       |     |      |      |      |      |      |      |      |      |      |
| Carbon-manganese-                     |      |       |     |      |      |      |      |      |      |      |      |      |
| silicon                               |      |       |     |      |      |      |      |      |      |      |      |      |
| (1% < Mn $\leq$ 1.65%,                |      |       |     |      |      |      |      |      |      |      |      |      |
| 0.1% < Si $\leq$ 0.6%)                |      |       |     |      |      |      |      |      |      |      |      |      |
| Chromium (low) steels                 |      |       |     |      |      |      |      |      |      |      |      |      |
| $\frac{1}{2}$ Cr- $\frac{1}{4}$ Mo-Si |      |       |     |      |      |      |      |      |      |      |      |      |
| (0.18% C, 0.65% Cr,                   |      |       |     |      |      |      |      |      |      |      |      |      |
| 0.23% Mo, 0.6% Si)                    |      |       |     |      |      |      |      |      |      |      |      |      |
| 1Cr- $\frac{1}{2}$ Mo                 |      |       |     |      |      |      |      |      |      |      |      |      |
| (0.16% C, 1% Cr,                      |      |       |     |      |      |      |      |      |      |      |      |      |
| 0.54% Mo, 0.39% Si)                   |      |       |     |      |      |      |      |      |      |      |      |      |
| 1Cr-V                                 |      |       |     |      |      |      |      |      |      |      |      |      |
| (0.2% C, 1.02% Cr,                    |      |       |     |      |      |      |      |      |      |      |      |      |
| 0.15% V)                              |      |       |     |      |      |      |      |      |      |      |      |      |
| Stainless steels                      |      |       |     |      |      |      |      |      |      |      |      |      |
| AISI 302                              |      |       |     |      |      |      |      |      |      |      |      |      |
|                                       | 8055 |       | 480 | 15.1 | 3.91 |      |      | 17.3 | 20.0 | 22.8 | 25.4 |      |
|                                       |      |       |     |      |      |      |      | 512  | 559  | 585  | 606  |      |
| AISI 304                              |      |       |     |      |      |      |      |      |      |      |      |      |
|                                       | 1670 |       | 477 | 14.9 | 3.95 | 9.2  | 12.6 | 16.6 | 19.8 | 22.6 | 25.4 | 28.0 |
|                                       |      |       |     |      |      | 272  | 402  | 515  | 557  | 582  | 611  | 640  |
| AISI 316                              |      |       |     |      |      |      |      |      |      |      |      |      |
|                                       | 8238 |       | 468 | 13.4 | 3.48 |      |      | 15.2 | 18.3 | 21.3 | 24.2 |      |
|                                       |      |       |     |      |      |      |      | 504  | 550  | 576  | 602  |      |
| AISI 347                              |      |       |     |      |      |      |      |      |      |      |      |      |
|                                       | 7978 |       | 480 | 14.2 | 3.71 |      |      | 15.8 | 18.9 | 21.9 | 24.7 |      |
|                                       |      |       |     |      |      |      |      | 513  | 559  | 585  | 606  |      |

TABLE A.1 Continued

| Composition                                   | Melting Point (K) | Properties at 300 K            |                     |                  |                                            | Properties at Various Temperatures (K) |      |      |      |      |      |      |      |      |      |
|-----------------------------------------------|-------------------|--------------------------------|---------------------|------------------|--------------------------------------------|----------------------------------------|------|------|------|------|------|------|------|------|------|
|                                               |                   | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(J/kg · K) | $k$<br>(W/m · K) | $\alpha \cdot 10^6$<br>(m <sup>2</sup> /s) | $k$ (W/m · K)/ $c_p$ (J/kg · K)        |      |      |      |      |      |      |      |      |      |
|                                               |                   |                                |                     |                  |                                            | 100                                    | 200  | 400  | 600  | 800  | 1000 | 1200 | 1500 | 2000 | 2500 |
| Lead                                          | 601               | 11340                          | 129                 | 35.3             | 24.1                                       | 39.7                                   | 36.7 | 34.0 | 31.4 |      |      |      |      |      |      |
|                                               |                   |                                |                     |                  |                                            | 118                                    | 125  | 132  | 142  |      |      |      |      |      |      |
| Magnesium                                     | 923               | 1740                           | 1024                | 156              | 87.6                                       | 169                                    | 159  | 153  | 149  | 146  |      |      |      |      |      |
|                                               |                   |                                |                     |                  |                                            | 649                                    | 934  | 1074 | 1170 | 1267 |      |      |      |      |      |
| Molybdenum                                    | 2894              | 10240                          | 251                 | 138              | 53.7                                       | 179                                    | 143  | 134  | 126  | 118  | 112  | 105  | 98   | 90   | 86   |
|                                               |                   |                                |                     |                  |                                            | 141                                    | 224  | 261  | 275  | 285  | 295  | 308  | 330  | 380  | 459  |
| Nickel                                        |                   |                                |                     |                  |                                            |                                        |      |      |      |      |      |      |      |      |      |
| Pure                                          | 1728              | 8900                           | 444                 | 90.7             | 23.0                                       | 164                                    | 107  | 80.2 | 65.6 | 67.6 | 71.8 | 76.2 | 82.6 |      |      |
|                                               |                   |                                |                     |                  |                                            | 232                                    | 383  | 485  | 592  | 530  | 562  | 594  | 616  |      |      |
| Nichrome<br>(80% Ni, 20% Cr)                  | 1672              | 8400                           | 420                 | 12               | 3.4                                        |                                        |      | 14   | 16   | 21   |      |      |      |      |      |
| Inconel X-750<br>(73% Ni, 15% Cr,<br>6.7% Fe) | 1665              | 8510                           | 439                 | 11.7             | 3.1                                        | 8.7                                    | 10.3 | 13.5 | 17.0 | 20.5 | 24.0 | 27.6 | 33.0 |      |      |
|                                               |                   |                                |                     |                  |                                            | —                                      | 372  | 473  | 510  | 546  | 626  | —    | —    |      |      |
| Niobium                                       | 2741              | 8570                           | 265                 | 53.7             | 23.6                                       | 55.2                                   | 52.6 | 55.2 | 58.2 | 61.3 | 64.4 | 67.5 | 72.1 | 79.1 |      |
|                                               |                   |                                |                     |                  |                                            | 188                                    | 249  | 274  | 283  | 292  | 301  | 310  | 324  | 347  |      |
| Palladium                                     | 1827              | 12020                          | 244                 | 71.8             | 24.5                                       | 76.5                                   | 71.6 | 73.6 | 79.7 | 86.9 | 94.2 | 102  | 110  |      |      |
|                                               |                   |                                |                     |                  |                                            | 168                                    | 227  | 251  | 261  | 271  | 281  | 291  | 307  |      |      |
| Platinum                                      |                   |                                |                     |                  |                                            |                                        |      |      |      |      |      |      |      |      |      |
| Pure                                          | 2045              | 21450                          | 133                 | 71.6             | 25.1                                       | 77.5                                   | 72.6 | 71.8 | 73.2 | 75.6 | 78.7 | 82.6 | 89.5 | 99.4 |      |
|                                               |                   |                                |                     |                  |                                            | 100                                    | 125  | 136  | 141  | 146  | 152  | 157  | 165  | 179  |      |
| Alloy 60Pt-40Rh<br>(60% Pt, 40% Rh)           | 1800              | 16630                          | 162                 | 47               | 17.4                                       |                                        |      | 52   | 59   | 65   | 69   | 73   | 76   |      |      |
| Rhenium                                       | 3453              | 21100                          | 136                 | 47.9             | 16.7                                       | 58.9                                   | 51.0 | 46.1 | 44.2 | 44.1 | 44.6 | 45.7 | 47.8 | 51.9 |      |
|                                               |                   |                                |                     |                  |                                            | 97                                     | 127  | 139  | 145  | 151  | 156  | 162  | 171  | 186  |      |
| Rhodium                                       | 2236              | 12450                          | 243                 | 150              | 49.6                                       | 186                                    | 154  | 146  | 136  | 127  | 121  | 116  | 110  | 112  |      |
|                                               |                   |                                |                     |                  |                                            | 147                                    | 220  | 253  | 274  | 293  | 311  | 327  | 349  | 376  |      |
| Silicon                                       | 1685              | 2330                           | 712                 | 148              | 89.2                                       | 884                                    | 264  | 98.9 | 61.9 | 42.2 | 31.2 | 25.7 | 22.7 |      |      |
|                                               |                   |                                |                     |                  |                                            | 259                                    | 556  | 790  | 867  | 913  | 946  | 967  | 992  |      |      |
| Silver                                        | 1235              | 10500                          | 235                 | 429              | 174                                        | 444                                    | 430  | 425  | 412  | 396  | 379  | 361  |      |      |      |
|                                               |                   |                                |                     |                  |                                            | 187                                    | 225  | 239  | 250  | 262  | 277  | 292  |      |      |      |
| Tantalum                                      | 3269              | 16600                          | 140                 | 57.5             | 24.7                                       | 59.2                                   | 57.5 | 57.8 | 58.6 | 59.4 | 60.2 | 61.0 | 62.2 | 64.1 | 65.6 |
|                                               |                   |                                |                     |                  |                                            | 110                                    | 133  | 144  | 146  | 149  | 152  | 155  | 160  | 172  | 189  |

|           |      |       |     |      |      |      |      |      |      |      |      |      |
|-----------|------|-------|-----|------|------|------|------|------|------|------|------|------|
| Thorium   | 2023 | 11700 | 118 | 54.0 | 39.1 | 59.8 | 54.6 | 54.5 | 55.8 | 56.9 | 56.9 | 58.7 |
| Tin       | 505  | 7310  | 227 | 66.6 | 40.1 | 59.9 | 54.6 | 54.5 | 55.8 | 56.9 | 56.9 | 58.7 |
|           |      |       |     |      |      | 99   | 112  | 124  | 134  | 145  | 156  | 167  |
| Titanium  | 1953 | 4500  | 522 | 21.9 | 9.32 | 85.2 | 73.3 | 62.2 |      |      |      |      |
|           |      |       |     |      |      | 188  | 215  | 243  |      |      |      |      |
| Tungsten  | 3660 | 19300 | 132 | 174  | 68.3 | 30.5 | 24.5 | 20.4 | 19.4 | 19.7 | 20.7 | 22.0 |
|           |      |       |     |      |      | 300  | 465  | 551  | 591  | 633  | 675  | 620  |
| Uranium   | 1406 | 19070 | 116 | 27.6 | 12.5 | 21.7 | 25.1 | 29.6 | 34.0 | 38.8 | 43.9 | 49.0 |
|           |      |       |     |      |      | 94   | 108  | 125  | 146  | 176  | 180  | 161  |
| Vanadium  | 2192 | 6100  | 489 | 30.7 | 10.3 | 35.8 | 31.3 | 31.3 | 33.3 | 35.7 | 38.2 | 40.8 |
|           |      |       |     |      |      | 258  | 430  | 515  | 540  | 563  | 597  | 645  |
| Zinc      | 693  | 7140  | 389 | 116  | 41.8 | 117  | 118  | 111  | 103  |      |      |      |
|           |      |       |     |      |      | 297  | 367  | 402  | 436  |      |      |      |
| Zirconium | 2125 | 6570  | 278 | 22.7 | 12.4 | 33.2 | 25.2 | 21.6 | 20.7 | 21.6 | 23.7 | 26.0 |
|           |      |       |     |      |      | 205  | 264  | 300  | 322  | 342  | 362  | 344  |

<sup>a</sup>Adapted from References 1-7.

**TABLE A.2** Thermophysical Properties of Selected Nonmetallic Solids<sup>a</sup>

| Composition                              | Melting Point (K) | Properties at 300 K         |                |             |                                         | Properties at Various Temperatures (K) |      |      |      |      |      |      |      |      |      |
|------------------------------------------|-------------------|-----------------------------|----------------|-------------|-----------------------------------------|----------------------------------------|------|------|------|------|------|------|------|------|------|
|                                          |                   | $\rho$ (kg/m <sup>3</sup> ) | $c_p$ (J/kg·K) | $k$ (W/m·K) | $\alpha \cdot 10^6$ (m <sup>2</sup> /s) | 100                                    | 200  | 400  | 600  | 800  | 1000 | 1200 | 1500 | 2000 | 2500 |
| Aluminum oxide, sapphire                 | 2323              | 3970                        | 765            | 46          | 15.1                                    | 450                                    | 82   | 32.4 | 18.9 | 13.0 | 10.5 |      |      |      |      |
|                                          |                   |                             |                |             |                                         | —                                      | —    | 940  | 1110 | 1180 | 1225 |      |      |      |      |
| Aluminum oxide, polycrystalline          | 2323              | 3970                        | 765            | 36.0        | 11.9                                    | 133                                    | 55   | 26.4 | 15.8 | 10.4 | 7.85 | 6.55 | 5.66 | 6.00 |      |
| Beryllium oxide                          | 2725              | 3000                        | 1030           | 272         | 88.0                                    | —                                      | —    | 940  | 1110 | 1180 | 1225 | —    | —    | —    |      |
|                                          |                   |                             |                |             |                                         |                                        |      | 196  | 111  | 70   | 47   | 33   | 21.5 | 15   |      |
| Boron                                    | 2573              | 2500                        | 1105           | 27.6        | 9.99                                    | 190                                    | 52.5 | 18.7 | 11.3 | 8.1  | 6.3  | 5.2  | 2145 | 2750 |      |
|                                          |                   |                             |                |             |                                         | —                                      | —    | 1490 | 1880 | 2135 | 2350 | 2555 |      |      |      |
| Boron fiber epoxy (30% vol) composite    | 590               | 2080                        |                |             |                                         |                                        |      |      |      |      |      |      |      |      |      |
| $k$ ,    to fibers                       |                   |                             |                | 2.29        |                                         | 2.10                                   | 2.23 | 2.28 |      |      |      |      |      |      |      |
| $k$ , $\perp$ to fibers                  |                   |                             |                | 0.59        |                                         | 0.37                                   | 0.49 | 0.60 |      |      |      |      |      |      |      |
| $c_p$                                    |                   |                             | 1122           |             |                                         | 364                                    | 757  | 1431 |      |      |      |      |      |      |      |
| Carbon                                   |                   |                             |                |             |                                         |                                        |      |      |      |      |      |      |      |      |      |
| Amorphous                                | 1500              | 1950                        | —              | 1.60        | —                                       | 0.67                                   | 1.18 | 1.89 | 2.19 | 2.37 | 2.53 | 2.84 | 3.48 |      |      |
| Diamond, type IIa                        | —                 | 3500                        | 509            | 2300        | —                                       | 10,000                                 | 4000 | 1540 |      |      |      |      |      |      |      |
| insulator                                |                   |                             |                |             |                                         | 21                                     | 194  | 853  |      |      |      |      |      |      |      |
| Graphite, pyrolytic                      | 2273              | 2210                        |                | 1950        |                                         | 4970                                   | 3230 | 1390 | 892  | 667  | 534  | 448  | 357  | 262  |      |
| $k$ ,    to layers                       |                   |                             |                | 5.70        |                                         | 16.8                                   | 9.23 | 4.09 | 2.68 | 2.01 | 1.60 | 1.34 | 1.08 | 0.81 |      |
| $k$ , $\perp$ to layers                  |                   |                             |                |             |                                         | 136                                    | 411  | 992  | 1406 | 1650 | 1793 | 1890 | 1974 | 2043 |      |
| $c_p$                                    |                   |                             | 709            |             |                                         |                                        |      |      |      |      |      |      |      |      |      |
| Graphite fiber epoxy (25% vol) composite | 450               | 1400                        |                |             |                                         |                                        |      |      |      |      |      |      |      |      |      |
| $k$ , heat flow    to fibers             |                   |                             |                | 11.1        |                                         | 5.7                                    | 8.7  | 13.0 |      |      |      |      |      |      |      |
| $k$ , heat flow $\perp$ to fibers        |                   |                             |                | 0.87        |                                         | 0.46                                   | 0.68 | 1.1  |      |      |      |      |      |      |      |
| $c_p$                                    |                   |                             | 935            |             |                                         | 337                                    | 642  | 1216 |      |      |      |      |      |      |      |
| Pyroceram, Corning 9606                  | 1623              | 2600                        | 808            | 3.98        | 1.89                                    | 5.25                                   | 4.78 | 3.64 | 3.28 | 3.08 | 2.96 | 2.87 | 2.79 |      |      |
|                                          |                   |                             |                |             |                                         | —                                      | —    | 908  | 1038 | 1122 | 1197 | 1264 | 1498 |      |      |

|                                                 |      |      |     |       |       |       |       |      |      |      |      |      |      |
|-------------------------------------------------|------|------|-----|-------|-------|-------|-------|------|------|------|------|------|------|
| Silicon carbide                                 | 3100 | 3160 | 675 | 490   | 230   | —     | 880   | —    | 1050 | 1135 | 87   | 58   | 30   |
| Silicon dioxide, crystalline (quartz)           | 1883 | 2650 |     |       |       |       |       |      |      |      | 1195 | 1243 | 1310 |
| $k$ , $\parallel$ to $c$ axis                   |      |      |     | 10.4  |       |       |       | 16.4 | 7.6  | 5.0  | 4.2  |      |      |
| $k$ , $\perp$ to $c$ axis                       |      |      |     | 6.21  |       |       |       | 9.5  | 4.70 | 3.4  | 3.1  |      |      |
| $c_p$                                           |      |      | 745 |       |       |       |       | —    | 885  | 1075 | 1250 |      |      |
| Silicon dioxide, polycrystalline (fused silica) | 1883 | 2220 | 745 | 1.38  | 0.834 | 0.69  | 1.14  | 1.51 | 1.75 | 2.17 | 2.87 | 4.00 |      |
| Silicon nitride                                 | 2173 | 2400 | 691 | 16.0  | 9.65  | —     | —     | —    | 13.9 | 11.3 | 9.88 | 8.00 | 7.16 |
| Sulfur                                          | 392  | 2070 | 708 | 0.206 | 0.141 | 0.165 | 0.185 | 578  | 778  | 937  | 1063 | 1226 | 1306 |
| Thorium dioxide                                 | 3573 | 9110 | 235 | 13    | 6.1   | 403   | 606   |      |      |      |      |      | 1377 |
| Titanium dioxide, polycrystalline               | 2133 | 4157 | 710 | 8.4   | 2.8   |       |       |      | 10.2 | 6.6  | 4.7  | 3.68 | 3.12 |
|                                                 |      |      |     |       |       |       |       |      | 255  | 274  | 285  | 295  | 303  |
|                                                 |      |      |     |       |       |       |       |      | 7.01 | 5.02 | 3.94 | 3.46 | 3.28 |
|                                                 |      |      |     |       |       |       |       |      | 805  | 880  | 910  | 930  | 945  |

\*Adapted from References 1, 2, 3, and 6.

**TABLE A.3** Thermophysical Properties of Common Materials<sup>a</sup>*Structural Building Materials*

| Description/Composition               | Typical Properties at 300 K                |                                           |                                       |
|---------------------------------------|--------------------------------------------|-------------------------------------------|---------------------------------------|
|                                       | Density,<br>$\rho$<br>(kg/m <sup>3</sup> ) | Thermal<br>Conductivity, $k$<br>(W/m · K) | Specific<br>Heat, $c_p$<br>(J/kg · K) |
| <b>Building Boards</b>                |                                            |                                           |                                       |
| Asbestos–cement board                 | 1920                                       | 0.58                                      | —                                     |
| Gypsum or plaster board               | 800                                        | 0.17                                      | —                                     |
| Plywood                               | 545                                        | 0.12                                      | 1215                                  |
| Sheathing, regular density            | 290                                        | 0.055                                     | 1300                                  |
| Acoustic tile                         | 290                                        | 0.058                                     | 1340                                  |
| Hardboard, siding                     | 640                                        | 0.094                                     | 1170                                  |
| Hardboard, high density               | 1010                                       | 0.15                                      | 1380                                  |
| Particle board, low density           | 590                                        | 0.078                                     | 1300                                  |
| Particle board, high density          | 1000                                       | 0.170                                     | 1300                                  |
| <b>Woods</b>                          |                                            |                                           |                                       |
| Hardwoods (oak, maple)                | 720                                        | 0.16                                      | 1255                                  |
| Softwoods (fir, pine)                 | 510                                        | 0.12                                      | 1380                                  |
| <b>Masonry Materials</b>              |                                            |                                           |                                       |
| Cement mortar                         | 1860                                       | 0.72                                      | 780                                   |
| Brick, common                         | 1920                                       | 0.72                                      | 835                                   |
| Brick, face                           | 2083                                       | 1.3                                       | —                                     |
| Clay tile, hollow                     |                                            |                                           |                                       |
| 1 cell deep, 10 cm thick              | —                                          | 0.52                                      | —                                     |
| 3 cells deep, 30 cm thick             | —                                          | 0.69                                      | —                                     |
| Concrete block, 3 oval cores          |                                            |                                           |                                       |
| Sand/gravel, 20 cm thick              | —                                          | 1.0                                       | —                                     |
| Cinder aggregate, 20 cm thick         | —                                          | 0.67                                      | —                                     |
| Concrete block, rectangular core      |                                            |                                           |                                       |
| 2 cores, 20 cm thick, 16 kg           | —                                          | 1.1                                       | —                                     |
| Same with filled cores                | —                                          | 0.60                                      | —                                     |
| <b>Plastering Materials</b>           |                                            |                                           |                                       |
| Cement plaster, sand aggregate        | 1860                                       | 0.72                                      | —                                     |
| Gypsum plaster, sand aggregate        | 1680                                       | 0.22                                      | 1085                                  |
| Gypsum plaster, vermiculite aggregate | 720                                        | 0.25                                      | —                                     |

TABLE A.3 Continued

## Insulating Materials and Systems

| Description/Composition                                                                                 | Typical Properties at 300 K                |                                           |                                       |
|---------------------------------------------------------------------------------------------------------|--------------------------------------------|-------------------------------------------|---------------------------------------|
|                                                                                                         | Density,<br>$\rho$<br>(kg/m <sup>3</sup> ) | Thermal<br>Conductivity, $k$<br>(W/m · K) | Specific<br>Heat, $c_p$<br>(J/kg · K) |
| <b>Blanket and Batt</b>                                                                                 |                                            |                                           |                                       |
| Glass fiber, paper faced                                                                                | 16                                         | 0.046                                     | —                                     |
|                                                                                                         | 28                                         | 0.038                                     | —                                     |
|                                                                                                         | 40                                         | 0.035                                     | —                                     |
| Glass fiber, coated; duct liner                                                                         | 32                                         | 0.038                                     | 835                                   |
| <b>Board and Slab</b>                                                                                   |                                            |                                           |                                       |
| Cellular glass                                                                                          | 145                                        | 0.058                                     | 1000                                  |
| Glass fiber, organic bonded                                                                             | 105                                        | 0.036                                     | 795                                   |
| Polystyrene, expanded                                                                                   |                                            |                                           |                                       |
| Extruded (R-12)                                                                                         | 55                                         | 0.027                                     | 1210                                  |
| Molded beads                                                                                            | 16                                         | 0.040                                     | 1210                                  |
| Mineral fiberboard; roofing material                                                                    | 265                                        | 0.049                                     | —                                     |
| Wood, shredded/cemented                                                                                 | 350                                        | 0.087                                     | 1590                                  |
| Cork                                                                                                    | 120                                        | 0.039                                     | 1800                                  |
| <b>Loose Fill</b>                                                                                       |                                            |                                           |                                       |
| Cork, granulated                                                                                        | 160                                        | 0.045                                     | —                                     |
| Diatomaceous silica, coarse                                                                             | 350                                        | 0.069                                     | —                                     |
| Powder                                                                                                  | 400                                        | 0.091                                     | —                                     |
| Diatomaceous silica, fine powder                                                                        | 200                                        | 0.052                                     | —                                     |
|                                                                                                         | 275                                        | 0.061                                     | —                                     |
| Glass fiber, poured or blown                                                                            | 16                                         | 0.043                                     | 835                                   |
| Vermiculite, flakes                                                                                     | 80                                         | 0.068                                     | 835                                   |
|                                                                                                         | 160                                        | 0.063                                     | 1000                                  |
| <b>Formed/Foamed-in-Place</b>                                                                           |                                            |                                           |                                       |
| Mineral wool granules with asbestos/inorganic binders, sprayed                                          | 190                                        | 0.046                                     | —                                     |
| Polyvinyl acetate cork mastic; sprayed or troweled                                                      | —                                          | 0.100                                     | —                                     |
| Urethane, two-part mixture; rigid foam                                                                  | 70                                         | 0.026                                     | 1045                                  |
| <b>Reflective</b>                                                                                       |                                            |                                           |                                       |
| Aluminum foil separating fluffy glass mats; 10–12 layers, evacuated; for cryogenic applications (150 K) | 40                                         | 0.00016                                   | —                                     |
| Aluminum foil and glass paper laminate; 75–150 layers; evacuated; for cryogenic application (150 K)     | 120                                        | 0.000017                                  | —                                     |
| Typical silica powder, evacuated                                                                        | 160                                        | 0.0017                                    | —                                     |

TABLE A.3 Continued

| Industrial Insulation                   |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|-----------------------------------------|---------------------------------------|--------------------------------------------|-------------------------------------------------------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----|-----|-----|
| Description/<br>Composition             | Maximum<br>Service<br>Temperature (K) | Typical<br>Density<br>(kg/m <sup>3</sup> ) | Typical Thermal Conductivity, <i>k</i> (W/m · K), at Various Temperatures (K) |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            | 200                                                                           | 215   | 230   | 240   | 255   | 270   | 285   | 300   | 310   | 365   | 420   | 530 | 645 | 750 |
| Blankets                                |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Blanket, mineral fiber;                 | 920                                   | 96–192                                     |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| metal reinforced                        | 815                                   | 40–96                                      |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Blanket, mineral fiber;                 | 450                                   | 10                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| glass; fine fiber,                      |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| organic bonded                          |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 12                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 16                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 24                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 32                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 48                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Blanket, alumina–                       |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| silica fiber                            | 1530                                  | 48                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 64                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 96                                         |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       | 128                                        |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Felt, semirigid;                        | 480                                   | 50–125                                     |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| organic bonded                          | 730                                   | 50                                         | 0.023                                                                         | 0.025 | 0.026 | 0.027 | 0.029 | 0.030 | 0.032 | 0.033 | 0.035 | 0.051 | 0.079 |     |     |     |
| Felt, laminated;                        |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| no binder                               | 920                                   | 120                                        |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Blocks, Boards, and<br>Pipe Insulations |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Asbestos paper,                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| laminated and                           |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| corrugated                              |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| 4-ply                                   | 420                                   | 190                                        |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| 6-ply                                   | 420                                   | 255                                        |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| 8-ply                                   | 420                                   | 300                                        |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Magnesia, 85%                           | 590                                   | 185                                        |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
| Calcium silicate                        | 920                                   | 190                                        |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       |       |       |       |       |       |       |       |       |       |     |     |     |
|                                         |                                       |                                            |                                                                               |       | </    |       |       |       |       |       |       |       |       |     |     |     |

|                               |      |     |       |       |       |       |       |       |       |       |       |       |       |       |
|-------------------------------|------|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Cellular glass                | 700  | 145 | 0.046 | 0.048 | 0.051 | 0.052 | 0.055 | 0.058 | 0.062 | 0.069 | 0.079 | 0.092 | 0.098 | 0.104 |
| Diatomaceous silica           | 1145 | 345 |       |       |       |       |       |       |       |       |       | 0.101 | 0.100 | 0.115 |
|                               | 1310 | 385 |       |       |       |       |       |       |       |       |       |       |       |       |
| Polystyrene, rigid            |      |     |       |       |       |       |       |       |       |       |       |       |       |       |
| Extruded (R-12)               | 350  | 56  | 0.023 | 0.023 | 0.023 | 0.025 | 0.026 | 0.027 | 0.029 |       |       |       |       |       |
| Extruded (R-12)               | 350  | 35  | 0.023 | 0.023 | 0.025 | 0.026 | 0.027 | 0.029 |       |       |       |       |       |       |
| Molded beads                  | 350  | 16  | 0.026 | 0.029 | 0.030 | 0.033 | 0.036 | 0.038 | 0.040 |       |       |       |       |       |
| Rubber, rigid foamed          | 340  | 70  |       |       |       | 0.029 | 0.030 | 0.032 | 0.033 |       |       |       |       |       |
| Insulating Cement             |      |     |       |       |       |       |       |       |       |       |       |       |       |       |
| Mineral fiber                 |      |     |       |       |       |       |       |       |       |       |       |       |       |       |
| (rock, slag or glass)         |      |     |       |       |       |       |       |       |       |       |       |       |       |       |
| With clay binder              | 1255 | 430 |       |       |       |       |       |       | 0.071 | 0.079 | 0.088 | 0.105 | 0.123 |       |
| With hydraulic setting binder | 922  | 560 |       |       |       |       |       |       | 0.108 | 0.115 | 0.123 | 0.137 |       |       |
| Loose Fill                    |      |     |       |       |       |       |       |       |       |       |       |       |       |       |
| Cellulose, wood or paper pulp | —    | 45  |       |       |       |       | 0.038 | 0.039 | 0.042 |       |       |       |       |       |
| Perlite, expanded             | —    | 105 | 0.036 | 0.039 | 0.042 | 0.043 | 0.046 | 0.049 | 0.051 | 0.053 | 0.056 |       |       |       |
| Vermiculite, expanded         | —    | 122 |       |       |       |       |       |       |       |       |       |       |       |       |
|                               |      | 80  | 0.056 | 0.058 | 0.061 | 0.063 | 0.065 | 0.068 | 0.071 |       |       |       |       |       |
|                               |      |     | 0.049 | 0.051 | 0.055 | 0.058 | 0.061 | 0.063 | 0.066 |       |       |       |       |       |

TABLE A.3 Continued

| Other Materials                   |                    |                                            |                                           |                                       |
|-----------------------------------|--------------------|--------------------------------------------|-------------------------------------------|---------------------------------------|
| Description/<br>Composition       | Temperature<br>(K) | Density,<br>$\rho$<br>(kg/m <sup>3</sup> ) | Thermal<br>Conductivity, $k$<br>(W/m · K) | Specific<br>Heat, $c_p$<br>(J/kg · K) |
| Asphalt                           | 300                | 2115                                       | 0.062                                     | 920                                   |
| Bakelite                          | 300                | 1300                                       | 1.4                                       | 1465                                  |
| Brick, refractory                 |                    |                                            |                                           |                                       |
| Carborundum                       | 872                | —                                          | 18.5                                      | —                                     |
|                                   | 1672               | —                                          | 11.0                                      | —                                     |
| Chrome brick                      | 473                | 3010                                       | 2.3                                       | 835                                   |
|                                   | 823                |                                            | 2.5                                       |                                       |
|                                   | 1173               |                                            | 2.0                                       |                                       |
| Diatomaceous<br>silica, fired     | 478                | —                                          | 0.25                                      | —                                     |
|                                   | 1145               | —                                          | 0.30                                      |                                       |
| Fire clay, burnt 1600 K           | 773                | 2050                                       | 1.0                                       | 960                                   |
|                                   | 1073               | —                                          | 1.1                                       |                                       |
|                                   | 1373               | —                                          | 1.1                                       |                                       |
| Fire clay, burnt 1725 K           | 773                | 2325                                       | 1.3                                       | 960                                   |
|                                   | 1073               |                                            | 1.4                                       |                                       |
|                                   | 1373               |                                            | 1.4                                       |                                       |
| Fire clay brick                   | 478                | 2645                                       | 1.0                                       | 960                                   |
|                                   | 922                |                                            | 1.5                                       |                                       |
|                                   | 1478               |                                            | 1.8                                       |                                       |
| Magnesite                         | 478                | —                                          | 3.8                                       | 1130                                  |
|                                   | 922                | —                                          | 2.8                                       |                                       |
|                                   | 1478               |                                            | 1.9                                       |                                       |
| Clay                              | 300                | 1460                                       | 1.3                                       | 880                                   |
| Coal, anthracite                  | 300                | 1350                                       | 0.26                                      | 1260                                  |
| Concrete (stone mix)              | 300                | 2300                                       | 1.4                                       | 880                                   |
| Cotton                            | 300                | 80                                         | 0.06                                      | 1300                                  |
| Foodstuffs                        |                    |                                            |                                           |                                       |
| Banana (75.7%<br>water content)   | 300                | 980                                        | 0.481                                     | 3350                                  |
| Apple, red (75%<br>water content) | 300                | 840                                        | 0.513                                     | 3600                                  |
| Cake, batter                      | 300                | 720                                        | 0.223                                     | —                                     |
| Cake, fully baked                 | 300                | 280                                        | 0.121                                     | —                                     |
| Chicken meat, white               | 198                | —                                          | 1.60                                      | —                                     |
| (74.4% water content)             | 233                | —                                          | 1.49                                      |                                       |
|                                   | 253                |                                            | 1.35                                      |                                       |
|                                   | 263                |                                            | 1.20                                      |                                       |
|                                   | 273                |                                            | 0.476                                     |                                       |
|                                   | 283                |                                            | 0.480                                     |                                       |
|                                   | 293                |                                            | 0.489                                     |                                       |
| Glass                             |                    |                                            |                                           |                                       |
| Plate (soda lime)                 | 300                | 2500                                       | 1.4                                       | 750                                   |
| Pyrex                             | 300                | 2225                                       | 1.4                                       | 835                                   |

TABLE A.3 Continued

*Other Materials (Continued)*

| Description/<br>Composition | Temperature<br>(K) | Density,<br>$\rho$<br>(kg/m <sup>3</sup> ) | Thermal<br>Conductivity, $k$<br>(W/m · K) | Specific<br>Heat, $c_p$<br>(J/kg · K) |
|-----------------------------|--------------------|--------------------------------------------|-------------------------------------------|---------------------------------------|
| Ice                         | 273                | 920                                        | 1.88                                      | 2040                                  |
|                             | 253                | —                                          | 2.03                                      | 1945                                  |
| Leather (sole)              | 300                | 998                                        | 0.159                                     | —                                     |
| Paper                       | 300                | 930                                        | 0.180                                     | 1340                                  |
| Paraffin                    | 300                | 900                                        | 0.240                                     | 2890                                  |
| Rock                        |                    |                                            |                                           |                                       |
| Granite, Barre              | 300                | 2630                                       | 2.79                                      | 775                                   |
| Limestone, Salem            | 300                | 2320                                       | 2.15                                      | 810                                   |
| Marble, Halston             | 300                | 2680                                       | 2.80                                      | 830                                   |
| Quartzite, Sioux            | 300                | 2640                                       | 5.38                                      | 1105                                  |
| Sandstone, Berea            | 300                | 2150                                       | 2.90                                      | 745                                   |
| Rubber, vulcanized          |                    |                                            |                                           |                                       |
| Soft                        | 300                | 1100                                       | 0.13                                      | 2010                                  |
| Hard                        | 300                | 1190                                       | 0.16                                      | —                                     |
| Sand                        | 300                | 1515                                       | 0.27                                      | 800                                   |
| Soil                        | 300                | 2050                                       | 0.52                                      | 1840                                  |
| Snow                        | 273                | 110                                        | 0.049                                     | —                                     |
|                             |                    | 500                                        | 0.190                                     | —                                     |
| Teflon                      | 300                | 2200                                       | 0.35                                      | —                                     |
|                             | 400                | —                                          | 0.45                                      | —                                     |
| Tissue, human               |                    |                                            |                                           |                                       |
| Skin                        | 300                | —                                          | 0.37                                      | —                                     |
| Fat layer (adipose)         | 300                | —                                          | 0.2                                       | —                                     |
| Muscle                      | 300                | —                                          | 0.5                                       | —                                     |
| Wood, cross grain           |                    |                                            |                                           |                                       |
| Balsa                       | 300                | 140                                        | 0.055                                     | —                                     |
| Cypress                     | 300                | 465                                        | 0.097                                     | —                                     |
| Fir                         | 300                | 415                                        | 0.11                                      | 2720                                  |
| Oak                         | 300                | 545                                        | 0.17                                      | 2385                                  |
| Yellow pine                 | 300                | 640                                        | 0.15                                      | 2805                                  |
| White pine                  | 300                | 435                                        | 0.11                                      | —                                     |
| Wood, radial                |                    |                                            |                                           |                                       |
| Oak                         | 300                | 545                                        | 0.19                                      | 2385                                  |
| Fir                         | 300                | 420                                        | 0.14                                      | 2720                                  |

\*Adapted from References 1 and 8–13.

**TABLE A.4** Thermophysical Properties  
of Gases at Atmospheric Pressure<sup>a</sup>

| $T$<br>(K)                      | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(kJ/kg · K) | $\mu \cdot 10^7$<br>(N · s/m <sup>2</sup> ) | $\nu \cdot 10^6$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) | $\alpha \cdot 10^6$<br>(m <sup>2</sup> /s) | $Pr$  |
|---------------------------------|--------------------------------|----------------------|---------------------------------------------|-----------------------------------------|-----------------------------|--------------------------------------------|-------|
| <b>Air</b>                      |                                |                      |                                             |                                         |                             |                                            |       |
| 100                             | 3.5562                         | 1.032                | 71.1                                        | 2.00                                    | 9.34                        | 2.54                                       | 0.786 |
| 150                             | 2.3364                         | 1.012                | 103.4                                       | 4.426                                   | 13.8                        | 5.84                                       | 0.758 |
| 200                             | 1.7458                         | 1.007                | 132.5                                       | 7.590                                   | 18.1                        | 10.3                                       | 0.737 |
| 250                             | 1.3947                         | 1.006                | 159.6                                       | 11.44                                   | 22.3                        | 15.9                                       | 0.720 |
| 300                             | 1.1614                         | 1.007                | 184.6                                       | 15.89                                   | 26.3                        | 22.5                                       | 0.707 |
| 350                             | 0.9950                         | 1.009                | 208.2                                       | 20.92                                   | 30.0                        | 29.9                                       | 0.700 |
| 400                             | 0.8711                         | 1.014                | 230.1                                       | 26.41                                   | 33.8                        | 38.3                                       | 0.690 |
| 450                             | 0.7740                         | 1.021                | 250.7                                       | 32.39                                   | 37.3                        | 47.2                                       | 0.686 |
| 500                             | 0.6964                         | 1.030                | 270.1                                       | 38.79                                   | 40.7                        | 56.7                                       | 0.684 |
| 550                             | 0.6329                         | 1.040                | 288.4                                       | 45.57                                   | 43.9                        | 66.7                                       | 0.683 |
| 600                             | 0.5804                         | 1.051                | 305.8                                       | 52.69                                   | 46.9                        | 76.9                                       | 0.685 |
| 650                             | 0.5356                         | 1.063                | 322.5                                       | 60.21                                   | 49.7                        | 87.3                                       | 0.690 |
| 700                             | 0.4975                         | 1.075                | 338.8                                       | 68.10                                   | 52.4                        | 98.0                                       | 0.695 |
| 750                             | 0.4643                         | 1.087                | 354.6                                       | 76.37                                   | 54.9                        | 109                                        | 0.702 |
| 800                             | 0.4354                         | 1.099                | 369.8                                       | 84.93                                   | 57.3                        | 120                                        | 0.709 |
| 850                             | 0.4097                         | 1.110                | 384.3                                       | 93.80                                   | 59.6                        | 131                                        | 0.716 |
| 900                             | 0.3868                         | 1.121                | 398.1                                       | 102.9                                   | 62.0                        | 143                                        | 0.720 |
| 950                             | 0.3666                         | 1.131                | 411.3                                       | 112.2                                   | 64.3                        | 155                                        | 0.723 |
| 1000                            | 0.3482                         | 1.141                | 424.4                                       | 121.9                                   | 66.7                        | 168                                        | 0.726 |
| 1100                            | 0.3166                         | 1.159                | 449.0                                       | 141.8                                   | 71.5                        | 195                                        | 0.728 |
| 1200                            | 0.2902                         | 1.175                | 473.0                                       | 162.9                                   | 76.3                        | 224                                        | 0.728 |
| 1300                            | 0.2679                         | 1.189                | 496.0                                       | 185.1                                   | 82                          | 238                                        | 0.719 |
| 1400                            | 0.2488                         | 1.207                | 530                                         | 213                                     | 91                          | 303                                        | 0.703 |
| 1500                            | 0.2322                         | 1.230                | 557                                         | 240                                     | 100                         | 350                                        | 0.685 |
| 1600                            | 0.2177                         | 1.248                | 584                                         | 268                                     | 106                         | 390                                        | 0.688 |
| 1700                            | 0.2049                         | 1.267                | 611                                         | 298                                     | 113                         | 435                                        | 0.685 |
| 1800                            | 0.1935                         | 1.286                | 637                                         | 329                                     | 120                         | 482                                        | 0.683 |
| 1900                            | 0.1833                         | 1.307                | 663                                         | 362                                     | 128                         | 534                                        | 0.677 |
| 2000                            | 0.1741                         | 1.337                | 689                                         | 396                                     | 137                         | 589                                        | 0.672 |
| 2100                            | 0.1658                         | 1.372                | 715                                         | 431                                     | 147                         | 646                                        | 0.667 |
| 2200                            | 0.1582                         | 1.417                | 740                                         | 468                                     | 160                         | 714                                        | 0.655 |
| 2300                            | 0.1513                         | 1.478                | 766                                         | 506                                     | 175                         | 783                                        | 0.647 |
| 2400                            | 0.1448                         | 1.558                | 792                                         | 547                                     | 196                         | 869                                        | 0.630 |
| 2500                            | 0.1389                         | 1.665                | 818                                         | 589                                     | 222                         | 960                                        | 0.613 |
| 3000                            | 0.1135                         | 2.726                | 955                                         | 841                                     | 486                         | 1570                                       | 0.536 |
| <b>Ammonia (NH<sub>3</sub>)</b> |                                |                      |                                             |                                         |                             |                                            |       |
| 300                             | 0.6894                         | 2.158                | 101.5                                       | 14.7                                    | 24.7                        | 16.6                                       | 0.887 |
| 320                             | 0.6448                         | 2.170                | 109                                         | 16.9                                    | 27.2                        | 19.4                                       | 0.870 |
| 340                             | 0.6059                         | 2.192                | 116.5                                       | 19.2                                    | 29.3                        | 22.1                                       | 0.872 |
| 360                             | 0.5716                         | 2.221                | 124                                         | 21.7                                    | 31.6                        | 24.9                                       | 0.872 |
| 380                             | 0.5410                         | 2.254                | 131                                         | 24.2                                    | 34.0                        | 27.9                                       | 0.869 |

TABLE A.4 Continued

| $T$<br>(K)                                  | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(kJ/kg · K) | $\mu \cdot 10^7$<br>(N · s/m <sup>2</sup> ) | $\nu \cdot 10^6$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) | $\alpha \cdot 10^6$<br>(m <sup>2</sup> /s) | $Pr$  |
|---------------------------------------------|--------------------------------|----------------------|---------------------------------------------|-----------------------------------------|-----------------------------|--------------------------------------------|-------|
| <b>Ammonia (NH<sub>3</sub>) (continued)</b> |                                |                      |                                             |                                         |                             |                                            |       |
| 400                                         | 0.5136                         | 2.287                | 138                                         | 26.9                                    | 37.0                        | 31.5                                       | 0.853 |
| 420                                         | 0.4888                         | 2.322                | 145                                         | 29.7                                    | 40.4                        | 35.6                                       | 0.833 |
| 440                                         | 0.4664                         | 2.357                | 152.5                                       | 32.7                                    | 43.5                        | 39.6                                       | 0.826 |
| 460                                         | 0.4460                         | 2.393                | 159                                         | 35.7                                    | 46.3                        | 43.4                                       | 0.822 |
| 480                                         | 0.4273                         | 2.430                | 166.5                                       | 39.0                                    | 49.2                        | 47.4                                       | 0.822 |
| 500                                         | 0.4101                         | 2.467                | 173                                         | 42.2                                    | 52.5                        | 51.9                                       | 0.813 |
| 520                                         | 0.3942                         | 2.504                | 180                                         | 45.7                                    | 54.5                        | 55.2                                       | 0.827 |
| 540                                         | 0.3795                         | 2.540                | 186.5                                       | 49.1                                    | 57.5                        | 59.7                                       | 0.824 |
| 560                                         | 0.3708                         | 2.577                | 193                                         | 52.0                                    | 60.6                        | 63.4                                       | 0.827 |
| 580                                         | 0.3533                         | 2.613                | 199.5                                       | 56.5                                    | 63.8                        | 69.1                                       | 0.817 |
| <b>Carbon Dioxide (CO<sub>2</sub>)</b>      |                                |                      |                                             |                                         |                             |                                            |       |
| 280                                         | 1.9022                         | 0.830                | 140                                         | 7.36                                    | 15.20                       | 9.63                                       | 0.765 |
| 300                                         | 1.7730                         | 0.851                | 149                                         | 8.40                                    | 16.55                       | 11.0                                       | 0.766 |
| 320                                         | 1.6609                         | 0.872                | 156                                         | 9.39                                    | 18.05                       | 12.5                                       | 0.754 |
| 340                                         | 1.5618                         | 0.891                | 165                                         | 10.6                                    | 19.70                       | 14.2                                       | 0.746 |
| 360                                         | 1.4743                         | 0.908                | 173                                         | 11.7                                    | 21.2                        | 15.8                                       | 0.741 |
| 380                                         | 1.3961                         | 0.926                | 181                                         | 13.0                                    | 22.75                       | 17.6                                       | 0.737 |
| 400                                         | 1.3257                         | 0.942                | 190                                         | 14.3                                    | 24.3                        | 19.5                                       | 0.737 |
| 450                                         | 1.1782                         | 0.981                | 210                                         | 17.8                                    | 28.3                        | 24.5                                       | 0.728 |
| 500                                         | 1.0594                         | 1.02                 | 231                                         | 21.8                                    | 32.5                        | 30.1                                       | 0.725 |
| 550                                         | 0.9625                         | 1.05                 | 251                                         | 26.1                                    | 36.6                        | 36.2                                       | 0.721 |
| 600                                         | 0.8826                         | 1.08                 | 270                                         | 30.6                                    | 40.7                        | 42.7                                       | 0.717 |
| 650                                         | 0.8143                         | 1.10                 | 288                                         | 35.4                                    | 44.5                        | 49.7                                       | 0.712 |
| 700                                         | 0.7564                         | 1.13                 | 305                                         | 40.3                                    | 48.1                        | 56.3                                       | 0.717 |
| 750                                         | 0.7057                         | 1.15                 | 321                                         | 45.5                                    | 51.7                        | 63.7                                       | 0.714 |
| 800                                         | 0.6614                         | 1.17                 | 337                                         | 51.0                                    | 55.1                        | 71.2                                       | 0.716 |
| <b>Carbon Monoxide (CO)</b>                 |                                |                      |                                             |                                         |                             |                                            |       |
| 200                                         | 1.6888                         | 1.045                | 127                                         | 7.52                                    | 17.0                        | 9.63                                       | 0.781 |
| 220                                         | 1.5341                         | 1.044                | 137                                         | 8.93                                    | 19.0                        | 11.9                                       | 0.753 |
| 240                                         | 1.4055                         | 1.043                | 147                                         | 10.5                                    | 20.6                        | 14.1                                       | 0.744 |
| 260                                         | 1.2967                         | 1.043                | 157                                         | 12.1                                    | 22.1                        | 16.3                                       | 0.741 |
| 280                                         | 1.2038                         | 1.042                | 166                                         | 13.8                                    | 23.6                        | 18.8                                       | 0.733 |
| 300                                         | 1.1233                         | 1.043                | 175                                         | 15.6                                    | 25.0                        | 21.3                                       | 0.730 |
| 320                                         | 1.0529                         | 1.043                | 184                                         | 17.5                                    | 26.3                        | 23.9                                       | 0.730 |
| 340                                         | 0.9909                         | 1.044                | 193                                         | 19.5                                    | 27.8                        | 26.9                                       | 0.725 |
| 360                                         | 0.9357                         | 1.045                | 202                                         | 21.6                                    | 29.1                        | 29.8                                       | 0.725 |
| 380                                         | 0.8864                         | 1.047                | 210                                         | 23.7                                    | 30.5                        | 32.9                                       | 0.729 |
| 400                                         | 0.8421                         | 1.049                | 218                                         | 25.9                                    | 31.8                        | 36.0                                       | 0.719 |
| 450                                         | 0.7483                         | 1.055                | 237                                         | 31.7                                    | 35.0                        | 44.3                                       | 0.714 |
| 500                                         | 0.67352                        | 1.065                | 254                                         | 37.7                                    | 38.1                        | 53.1                                       | 0.710 |
| 550                                         | 0.61226                        | 1.076                | 271                                         | 44.3                                    | 41.1                        | 62.4                                       | 0.710 |
| 600                                         | 0.56126                        | 1.088                | 286                                         | 51.0                                    | 44.0                        | 72.1                                       | 0.707 |

TABLE A.4 Continued

| $T$<br>(K)                              | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(kJ/kg · K) | $\mu \cdot 10^7$<br>(N · s/m <sup>2</sup> ) | $\nu \cdot 10^6$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) | $\alpha \cdot 10^6$<br>(m <sup>2</sup> /s) | $Pr$  |
|-----------------------------------------|--------------------------------|----------------------|---------------------------------------------|-----------------------------------------|-----------------------------|--------------------------------------------|-------|
| <b>Carbon Monoxide (CO) (continued)</b> |                                |                      |                                             |                                         |                             |                                            |       |
| 650                                     | 0.51806                        | 1.101                | 301                                         | 58.1                                    | 47.0                        | 82.4                                       | 0.705 |
| 700                                     | 0.48102                        | 1.114                | 315                                         | 65.5                                    | 50.0                        | 93.3                                       | 0.702 |
| 750                                     | 0.44899                        | 1.127                | 329                                         | 73.3                                    | 52.8                        | 104                                        | 0.702 |
| 800                                     | 0.42095                        | 1.140                | 343                                         | 81.5                                    | 55.5                        | 116                                        | 0.705 |
| <b>Helium (He)</b>                      |                                |                      |                                             |                                         |                             |                                            |       |
| 100                                     | 0.4871                         | 5.193                | 96.3                                        | 19.8                                    | 73.0                        | 28.9                                       | 0.686 |
| 120                                     | 0.4060                         | 5.193                | 107                                         | 26.4                                    | 81.9                        | 38.8                                       | 0.679 |
| 140                                     | 0.3481                         | 5.193                | 118                                         | 33.9                                    | 90.7                        | 50.2                                       | 0.676 |
| 160                                     | —                              | 5.193                | 129                                         | —                                       | 99.2                        | —                                          | —     |
| 180                                     | 0.2708                         | 5.193                | 139                                         | 51.3                                    | 107.2                       | 76.2                                       | 0.673 |
| 200                                     | —                              | 5.193                | 150                                         | —                                       | 115.1                       | —                                          | —     |
| 220                                     | 0.2216                         | 5.193                | 160                                         | 72.2                                    | 123.1                       | 107                                        | 0.675 |
| 240                                     | —                              | 5.193                | 170                                         | —                                       | 130                         | —                                          | —     |
| 260                                     | 0.1875                         | 5.193                | 180                                         | 96.0                                    | 137                         | 141                                        | 0.682 |
| 280                                     | —                              | 5.193                | 190                                         | —                                       | 145                         | —                                          | —     |
| 300                                     | 0.1625                         | 5.193                | 199                                         | 122                                     | 152                         | 180                                        | 0.680 |
| 350                                     | —                              | 5.193                | 221                                         | —                                       | 170                         | —                                          | —     |
| 400                                     | 0.1219                         | 5.193                | 243                                         | 199                                     | 187                         | 295                                        | 0.675 |
| 450                                     | —                              | 5.193                | 263                                         | —                                       | 204                         | —                                          | —     |
| 500                                     | 0.09754                        | 5.193                | 283                                         | 290                                     | 220                         | 434                                        | 0.668 |
| 550                                     | —                              | 5.193                | —                                           | —                                       | —                           | —                                          | —     |
| 600                                     | —                              | 5.193                | 320                                         | —                                       | 252                         | —                                          | —     |
| 650                                     | —                              | 5.193                | 332                                         | —                                       | 264                         | —                                          | —     |
| 700                                     | 0.06969                        | 5.193                | 350                                         | 502                                     | 278                         | 768                                        | 0.654 |
| 750                                     | —                              | 5.193                | 364                                         | —                                       | 291                         | —                                          | —     |
| 800                                     | —                              | 5.193                | 382                                         | —                                       | 304                         | —                                          | —     |
| 900                                     | —                              | 5.193                | 414                                         | —                                       | 330                         | —                                          | —     |
| 1000                                    | 0.04879                        | 5.193                | 446                                         | 914                                     | 354                         | 1400                                       | 0.654 |
| <b>Hydrogen (H<sub>2</sub>)</b>         |                                |                      |                                             |                                         |                             |                                            |       |
| 100                                     | 0.24255                        | 11.23                | 42.1                                        | 17.4                                    | 67.0                        | 24.6                                       | 0.707 |
| 150                                     | 0.16156                        | 12.60                | 56.0                                        | 34.7                                    | 101                         | 49.6                                       | 0.699 |
| 200                                     | 0.12115                        | 13.54                | 68.1                                        | 56.2                                    | 131                         | 79.9                                       | 0.704 |
| 250                                     | 0.09693                        | 14.06                | 78.9                                        | 81.4                                    | 157                         | 115                                        | 0.707 |
| 300                                     | 0.08078                        | 14.31                | 89.6                                        | 111                                     | 183                         | 158                                        | 0.701 |
| 350                                     | 0.06924                        | 14.43                | 98.8                                        | 143                                     | 204                         | 204                                        | 0.700 |
| 400                                     | 0.06059                        | 14.48                | 108.2                                       | 179                                     | 226                         | 258                                        | 0.695 |
| 450                                     | 0.05386                        | 14.50                | 117.2                                       | 218                                     | 247                         | 316                                        | 0.689 |
| 500                                     | 0.04848                        | 14.52                | 126.4                                       | 261                                     | 266                         | 378                                        | 0.691 |
| 550                                     | 0.04407                        | 14.53                | 134.3                                       | 305                                     | 285                         | 445                                        | 0.685 |

TABLE A.4 Continued

| $T$<br>(K)                                  | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(kJ/kg · K) | $\mu \cdot 10^7$<br>(N · s/m <sup>2</sup> ) | $\nu \cdot 10^6$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) | $\alpha \cdot 10^6$<br>(m <sup>2</sup> /s) | $Pr$  |
|---------------------------------------------|--------------------------------|----------------------|---------------------------------------------|-----------------------------------------|-----------------------------|--------------------------------------------|-------|
| <b>Hydrogen (H<sub>2</sub>) (continued)</b> |                                |                      |                                             |                                         |                             |                                            |       |
| 600                                         | 0.04040                        | 14.55                | 142.4                                       | 352                                     | 305                         | 519                                        | 0.678 |
| 700                                         | 0.03463                        | 14.61                | 157.8                                       | 456                                     | 342                         | 676                                        | 0.675 |
| 800                                         | 0.03030                        | 14.70                | 172.4                                       | 569                                     | 378                         | 849                                        | 0.670 |
| 900                                         | 0.02694                        | 14.83                | 186.5                                       | 692                                     | 412                         | 1030                                       | 0.671 |
| 1000                                        | 0.02424                        | 14.99                | 201.3                                       | 830                                     | 448                         | 1230                                       | 0.673 |
| 1100                                        | 0.02204                        | 15.17                | 213.0                                       | 966                                     | 488                         | 1460                                       | 0.662 |
| 1200                                        | 0.02020                        | 15.37                | 226.2                                       | 1120                                    | 528                         | 1700                                       | 0.659 |
| 1300                                        | 0.01865                        | 15.59                | 238.5                                       | 1279                                    | 568                         | 1955                                       | 0.655 |
| 1400                                        | 0.01732                        | 15.81                | 250.7                                       | 1447                                    | 610                         | 2230                                       | 0.650 |
| 1500                                        | 0.01616                        | 16.02                | 262.7                                       | 1626                                    | 655                         | 2530                                       | 0.643 |
| 1600                                        | 0.0152                         | 16.28                | 273.7                                       | 1801                                    | 697                         | 2815                                       | 0.639 |
| 1700                                        | 0.0143                         | 16.58                | 284.9                                       | 1992                                    | 742                         | 3130                                       | 0.637 |
| 1800                                        | 0.0135                         | 16.96                | 296.1                                       | 2193                                    | 786                         | 3435                                       | 0.639 |
| 1900                                        | 0.0128                         | 17.49                | 307.2                                       | 2400                                    | 835                         | 3730                                       | 0.643 |
| 2000                                        | 0.0121                         | 18.25                | 318.2                                       | 2630                                    | 878                         | 3975                                       | 0.661 |
| <b>Nitrogen (N<sub>2</sub>)</b>             |                                |                      |                                             |                                         |                             |                                            |       |
| 100                                         | 3.4388                         | 1.070                | 68.8                                        | 2.00                                    | 9.58                        | 2.60                                       | 0.768 |
| 150                                         | 2.2594                         | 1.050                | 100.6                                       | 4.45                                    | 13.9                        | 5.86                                       | 0.759 |
| 200                                         | 1.6883                         | 1.043                | 129.2                                       | 7.65                                    | 18.3                        | 10.4                                       | 0.736 |
| 250                                         | 1.3488                         | 1.042                | 154.9                                       | 11.48                                   | 22.2                        | 15.8                                       | 0.727 |
| 300                                         | 1.1233                         | 1.041                | 178.2                                       | 15.86                                   | 25.9                        | 22.1                                       | 0.716 |
| 350                                         | 0.9625                         | 1.042                | 200.0                                       | 20.78                                   | 29.3                        | 29.2                                       | 0.711 |
| 400                                         | 0.8425                         | 1.045                | 220.4                                       | 26.16                                   | 32.7                        | 37.1                                       | 0.704 |
| 450                                         | 0.7485                         | 1.050                | 239.6                                       | 32.01                                   | 35.8                        | 45.6                                       | 0.703 |
| 500                                         | 0.6739                         | 1.056                | 257.7                                       | 38.24                                   | 38.9                        | 54.7                                       | 0.700 |
| 550                                         | 0.6124                         | 1.065                | 274.7                                       | 44.86                                   | 41.7                        | 63.9                                       | 0.702 |
| 600                                         | 0.5615                         | 1.075                | 290.8                                       | 51.79                                   | 44.6                        | 73.9                                       | 0.701 |
| 700                                         | 0.4812                         | 1.098                | 321.0                                       | 66.71                                   | 49.9                        | 94.4                                       | 0.706 |
| 800                                         | 0.4211                         | 1.22                 | 349.1                                       | 82.90                                   | 54.8                        | 116                                        | 0.715 |
| 900                                         | 0.3743                         | 1.146                | 375.3                                       | 100.3                                   | 59.7                        | 139                                        | 0.721 |
| 1000                                        | 0.3368                         | 1.167                | 399.9                                       | 118.7                                   | 64.7                        | 165                                        | 0.721 |
| 1100                                        | 0.3062                         | 1.187                | 423.2                                       | 138.2                                   | 70.0                        | 193                                        | 0.718 |
| 1200                                        | 0.2807                         | 1.204                | 445.3                                       | 158.6                                   | 75.8                        | 224                                        | 0.707 |
| 1300                                        | 0.2591                         | 1.219                | 466.2                                       | 179.9                                   | 81.0                        | 256                                        | 0.701 |
| <b>Oxygen (O<sub>2</sub>)</b>               |                                |                      |                                             |                                         |                             |                                            |       |
| 100                                         | 3.945                          | 0.962                | 76.4                                        | 1.94                                    | 9.25                        | 2.44                                       | 0.796 |
| 150                                         | 2.585                          | 0.921                | 114.8                                       | 4.44                                    | 13.8                        | 5.80                                       | 0.766 |
| 200                                         | 1.930                          | 0.915                | 147.5                                       | 7.64                                    | 18.3                        | 10.4                                       | 0.737 |
| 250                                         | 1.542                          | 0.915                | 178.6                                       | 11.58                                   | 22.6                        | 16.0                                       | 0.723 |
| 300                                         | 1.284                          | 0.920                | 207.2                                       | 16.14                                   | 26.8                        | 22.7                                       | 0.711 |

TABLE A.4 Continued

| $T$<br>(K)                                | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(kJ/kg · K) | $\mu \cdot 10^7$<br>(N · s/m <sup>2</sup> ) | $\nu \cdot 10^6$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) | $\alpha \cdot 10^6$<br>(m <sup>2</sup> /s) | $Pr$  |
|-------------------------------------------|--------------------------------|----------------------|---------------------------------------------|-----------------------------------------|-----------------------------|--------------------------------------------|-------|
| <b>Oxygen (O<sub>2</sub>) (continued)</b> |                                |                      |                                             |                                         |                             |                                            |       |
| 350                                       | 1.100                          | 0.929                | 233.5                                       | 21.23                                   | 29.6                        | 29.0                                       | 0.733 |
| 400                                       | 0.9620                         | 0.942                | 258.2                                       | 26.84                                   | 33.0                        | 36.4                                       | 0.737 |
| 450                                       | 0.8554                         | 0.956                | 281.4                                       | 32.90                                   | 36.3                        | 44.4                                       | 0.741 |
| 500                                       | 0.7698                         | 0.972                | 303.3                                       | 39.40                                   | 41.2                        | 55.1                                       | 0.716 |
| 550                                       | 0.6998                         | 0.988                | 324.0                                       | 46.30                                   | 44.1                        | 63.8                                       | 0.726 |
| 600                                       | 0.6414                         | 1.003                | 343.7                                       | 53.59                                   | 47.3                        | 73.5                                       | 0.729 |
| 700                                       | 0.5498                         | 1.031                | 380.8                                       | 69.26                                   | 52.8                        | 93.1                                       | 0.744 |
| 800                                       | 0.4810                         | 1.054                | 415.2                                       | 86.32                                   | 58.9                        | 116                                        | 0.743 |
| 900                                       | 0.4275                         | 1.074                | 447.2                                       | 104.6                                   | 64.9                        | 141                                        | 0.740 |
| 1000                                      | 0.3848                         | 1.090                | 477.0                                       | 124.0                                   | 71.0                        | 169                                        | 0.733 |
| 1100                                      | 0.3498                         | 1.103                | 505.5                                       | 144.5                                   | 75.8                        | 196                                        | 0.736 |
| 1200                                      | 0.3206                         | 1.115                | 532.5                                       | 166.1                                   | 81.9                        | 229                                        | 0.725 |
| 1300                                      | 0.2960                         | 1.125                | 588.4                                       | 188.6                                   | 87.1                        | 262                                        | 0.721 |
| <b>Water Vapor (Steam)</b>                |                                |                      |                                             |                                         |                             |                                            |       |
| 380                                       | 0.5863                         | 2.060                | 127.1                                       | 21.68                                   | 24.6                        | 20.4                                       | 1.06  |
| 400                                       | 0.5542                         | 2.014                | 134.4                                       | 24.25                                   | 26.1                        | 23.4                                       | 1.04  |
| 450                                       | 0.4902                         | 1.980                | 152.5                                       | 31.11                                   | 29.9                        | 30.8                                       | 1.01  |
| 500                                       | 0.4405                         | 1.985                | 170.4                                       | 38.68                                   | 33.9                        | 38.8                                       | 0.998 |
| 550                                       | 0.4005                         | 1.997                | 188.4                                       | 47.04                                   | 37.9                        | 47.4                                       | 0.993 |
| 600                                       | 0.3652                         | 2.026                | 206.7                                       | 56.60                                   | 42.2                        | 57.0                                       | 0.993 |
| 650                                       | 0.3380                         | 2.056                | 224.7                                       | 66.48                                   | 46.4                        | 66.8                                       | 0.996 |
| 700                                       | 0.3140                         | 2.085                | 242.6                                       | 77.26                                   | 50.5                        | 77.1                                       | 1.00  |
| 750                                       | 0.2931                         | 2.119                | 260.4                                       | 88.84                                   | 54.9                        | 88.4                                       | 1.00  |
| 800                                       | 0.2739                         | 2.152                | 278.6                                       | 101.7                                   | 59.2                        | 100                                        | 1.01  |
| 850                                       | 0.2579                         | 2.186                | 296.9                                       | 115.1                                   | 63.7                        | 113                                        | 1.02  |

\*Adapted from References 8, 14, and 15.

**TABLE A.5** Thermophysical Properties of Saturated Fluids<sup>a</sup>

| <i>Saturated Liquids</i>                                            |                                |                      |                                             |                                         |                             |                                            |           |                                          |
|---------------------------------------------------------------------|--------------------------------|----------------------|---------------------------------------------|-----------------------------------------|-----------------------------|--------------------------------------------|-----------|------------------------------------------|
| <i>T</i><br>(K)                                                     | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(kJ/kg · K) | $\mu \cdot 10^2$<br>(N · s/m <sup>2</sup> ) | $\nu \cdot 10^6$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) | $\alpha \cdot 10^7$<br>(m <sup>2</sup> /s) | <i>Pr</i> | $\beta \cdot 10^3$<br>(K <sup>-1</sup> ) |
| <b>Engine Oil (Unused)</b>                                          |                                |                      |                                             |                                         |                             |                                            |           |                                          |
| 273                                                                 | 899.1                          | 1.796                | 385                                         | 4280                                    | 147                         | 0.910                                      | 47,000    | 0.70                                     |
| 280                                                                 | 895.3                          | 1.827                | 217                                         | 2430                                    | 144                         | 0.880                                      | 27,500    | 0.70                                     |
| 290                                                                 | 890.0                          | 1.868                | 99.9                                        | 1120                                    | 145                         | 0.872                                      | 12,900    | 0.70                                     |
| 300                                                                 | 884.1                          | 1.909                | 48.6                                        | 550                                     | 145                         | 0.859                                      | 6400      | 0.70                                     |
| 310                                                                 | 877.9                          | 1.951                | 25.3                                        | 288                                     | 145                         | 0.847                                      | 3400      | 0.70                                     |
| 320                                                                 | 871.8                          | 1.993                | 14.1                                        | 161                                     | 143                         | 0.823                                      | 1965      | 0.70                                     |
| 330                                                                 | 865.8                          | 2.035                | 8.36                                        | 96.6                                    | 141                         | 0.800                                      | 1205      | 0.70                                     |
| 340                                                                 | 859.9                          | 2.076                | 5.31                                        | 61.7                                    | 139                         | 0.779                                      | 793       | 0.70                                     |
| 350                                                                 | 853.9                          | 2.118                | 3.56                                        | 41.7                                    | 138                         | 0.763                                      | 546       | 0.70                                     |
| 360                                                                 | 847.8                          | 2.161                | 2.52                                        | 29.7                                    | 138                         | 0.753                                      | 395       | 0.70                                     |
| 370                                                                 | 841.8                          | 2.206                | 1.86                                        | 22.0                                    | 137                         | 0.738                                      | 300       | 0.70                                     |
| 380                                                                 | 836.0                          | 2.250                | 1.41                                        | 16.9                                    | 136                         | 0.723                                      | 233       | 0.70                                     |
| 390                                                                 | 830.6                          | 2.294                | 1.10                                        | 13.3                                    | 135                         | 0.709                                      | 187       | 0.70                                     |
| 400                                                                 | 825.1                          | 2.337                | 0.874                                       | 10.6                                    | 134                         | 0.695                                      | 152       | 0.70                                     |
| 410                                                                 | 818.9                          | 2.381                | 0.698                                       | 8.52                                    | 133                         | 0.682                                      | 125       | 0.70                                     |
| 420                                                                 | 812.1                          | 2.427                | 0.564                                       | 6.94                                    | 133                         | 0.675                                      | 103       | 0.70                                     |
| 430                                                                 | 806.5                          | 2.471                | 0.470                                       | 5.83                                    | 132                         | 0.662                                      | 88        | 0.70                                     |
| <b>Ethylene Glycol [C<sub>2</sub>H<sub>4</sub>(OH)<sub>2</sub>]</b> |                                |                      |                                             |                                         |                             |                                            |           |                                          |
| 273                                                                 | 1130.8                         | 2.294                | 6.51                                        | 57.6                                    | 242                         | 0.933                                      | 617       | 0.65                                     |
| 280                                                                 | 1125.8                         | 2.323                | 4.20                                        | 37.3                                    | 244                         | 0.933                                      | 400       | 0.65                                     |
| 290                                                                 | 1118.8                         | 2.368                | 2.47                                        | 22.1                                    | 248                         | 0.936                                      | 236       | 0.65                                     |
| 300                                                                 | 1114.4                         | 2.415                | 1.57                                        | 14.1                                    | 252                         | 0.939                                      | 151       | 0.65                                     |
| 310                                                                 | 1103.7                         | 2.460                | 1.07                                        | 9.65                                    | 255                         | 0.939                                      | 103       | 0.65                                     |
| 320                                                                 | 1096.2                         | 2.505                | 0.757                                       | 6.91                                    | 258                         | 0.940                                      | 73.5      | 0.65                                     |
| 330                                                                 | 1089.5                         | 2.549                | 0.561                                       | 5.15                                    | 260                         | 0.936                                      | 55.0      | 0.65                                     |
| 340                                                                 | 1083.8                         | 2.592                | 0.431                                       | 3.98                                    | 261                         | 0.929                                      | 42.8      | 0.65                                     |
| 350                                                                 | 1079.0                         | 2.637                | 0.342                                       | 3.17                                    | 261                         | 0.917                                      | 34.6      | 0.65                                     |
| 360                                                                 | 1074.0                         | 2.682                | 0.278                                       | 2.59                                    | 261                         | 0.906                                      | 28.6      | 0.65                                     |
| 370                                                                 | 1066.7                         | 2.728                | 0.228                                       | 2.14                                    | 262                         | 0.900                                      | 23.7      | 0.65                                     |
| 373                                                                 | 1058.5                         | 2.742                | 0.215                                       | 2.03                                    | 263                         | 0.906                                      | 22.4      | 0.65                                     |
| <b>Glycerin [C<sub>3</sub>H<sub>8</sub>(OH)<sub>3</sub>]</b>        |                                |                      |                                             |                                         |                             |                                            |           |                                          |
| 273                                                                 | 1276.0                         | 2.261                | 1060                                        | 8310                                    | 282                         | 0.977                                      | 85,000    | 0.47                                     |
| 280                                                                 | 1271.9                         | 2.298                | 534                                         | 4200                                    | 284                         | 0.972                                      | 43,200    | 0.47                                     |
| 290                                                                 | 1265.8                         | 2.367                | 185                                         | 1460                                    | 286                         | 0.955                                      | 15,300    | 0.48                                     |
| 300                                                                 | 1259.9                         | 2.427                | 79.9                                        | 634                                     | 286                         | 0.935                                      | 6780      | 0.48                                     |
| 310                                                                 | 1253.9                         | 2.490                | 35.2                                        | 281                                     | 286                         | 0.916                                      | 3060      | 0.49                                     |
| 320                                                                 | 1247.2                         | 2.564                | 21.0                                        | 168                                     | 287                         | 0.897                                      | 1870      | 0.50                                     |

TABLE A.5 Continued

## Saturated Liquids (Continued)

| $T$<br>(K)                                                        | $\rho$<br>(kg/m <sup>3</sup> ) | $c_p$<br>(kJ/kg · K) | $\mu \cdot 10^2$<br>(N · s/m <sup>2</sup> ) | $\nu \cdot 10^6$<br>(m <sup>2</sup> /s) | $k \cdot 10^3$<br>(W/m · K) | $\alpha \cdot 10^7$<br>(m <sup>2</sup> /s) | $Pr$   | $\beta \cdot 10^3$<br>(K <sup>-1</sup> ) |
|-------------------------------------------------------------------|--------------------------------|----------------------|---------------------------------------------|-----------------------------------------|-----------------------------|--------------------------------------------|--------|------------------------------------------|
| <b>Refrigerant-134a (C<sub>2</sub>H<sub>2</sub>F<sub>4</sub>)</b> |                                |                      |                                             |                                         |                             |                                            |        |                                          |
| 230                                                               | 1426.8                         | 1.249                | 0.04912                                     | 0.3443                                  | 112.1                       | 0.629                                      | 5.5    | 2.02                                     |
| 240                                                               | 1397.7                         | 1.267                | 0.04202                                     | 0.3006                                  | 107.3                       | 0.606                                      | 5.0    | 2.11                                     |
| 250                                                               | 1367.9                         | 1.287                | 0.03633                                     | 0.2656                                  | 102.5                       | 0.583                                      | 4.6    | 2.23                                     |
| 260                                                               | 1337.1                         | 1.308                | 0.03166                                     | 0.2368                                  | 97.9                        | 0.560                                      | 4.2    | 2.36                                     |
| 270                                                               | 1305.1                         | 1.333                | 0.02775                                     | 0.2127                                  | 93.4                        | 0.537                                      | 4.0    | 2.53                                     |
| 280                                                               | 1271.8                         | 1.361                | 0.02443                                     | 0.1921                                  | 89.0                        | 0.514                                      | 3.7    | 2.73                                     |
| 290                                                               | 1236.8                         | 1.393                | 0.02156                                     | 0.1744                                  | 84.6                        | 0.491                                      | 3.5    | 2.98                                     |
| 300                                                               | 1199.7                         | 1.432                | 0.01905                                     | 0.1588                                  | 80.3                        | 0.468                                      | 3.4    | 3.30                                     |
| 310                                                               | 1159.9                         | 1.481                | 0.01680                                     | 0.1449                                  | 76.1                        | 0.443                                      | 3.3    | 3.73                                     |
| 320                                                               | 1116.8                         | 1.543                | 0.01478                                     | 0.1323                                  | 71.8                        | 0.417                                      | 3.2    | 4.33                                     |
| 330                                                               | 1069.1                         | 1.627                | 0.01292                                     | 0.1209                                  | 67.5                        | 0.388                                      | 3.1    | 5.19                                     |
| 340                                                               | 1015.0                         | 1.751                | 0.01118                                     | 0.1102                                  | 63.1                        | 0.355                                      | 3.1    | 6.57                                     |
| 350                                                               | 951.3                          | 1.961                | 0.00951                                     | 0.1000                                  | 58.6                        | 0.314                                      | 3.2    | 9.10                                     |
| 360                                                               | 870.1                          | 2.437                | 0.00781                                     | 0.0898                                  | 54.1                        | 0.255                                      | 3.5    | 15.39                                    |
| 370                                                               | 740.3                          | 5.105                | 0.00580                                     | 0.0783                                  | 51.8                        | 0.137                                      | 5.7    | 55.24                                    |
| <b>Refrigerant-22 (CHClF<sub>2</sub>)</b>                         |                                |                      |                                             |                                         |                             |                                            |        |                                          |
| 230                                                               | 1416.0                         | 1.087                | 0.03558                                     | 0.2513                                  | 114.5                       | 0.744                                      | 3.4    | 2.05                                     |
| 240                                                               | 1386.6                         | 1.100                | 0.03145                                     | 0.2268                                  | 109.8                       | 0.720                                      | 3.2    | 2.16                                     |
| 250                                                               | 1356.3                         | 1.117                | 0.02796                                     | 0.2062                                  | 105.2                       | 0.695                                      | 3.0    | 2.29                                     |
| 260                                                               | 1324.9                         | 1.137                | 0.02497                                     | 0.1884                                  | 100.7                       | 0.668                                      | 2.8    | 2.45                                     |
| 270                                                               | 1292.1                         | 1.161                | 0.02235                                     | 0.1730                                  | 96.2                        | 0.641                                      | 2.7    | 2.63                                     |
| 280                                                               | 1257.9                         | 1.189                | 0.02005                                     | 0.1594                                  | 91.7                        | 0.613                                      | 2.6    | 2.86                                     |
| 290                                                               | 1221.7                         | 1.223                | 0.01798                                     | 0.1472                                  | 87.2                        | 0.583                                      | 2.5    | 3.15                                     |
| 300                                                               | 1183.4                         | 1.265                | 0.01610                                     | 0.1361                                  | 82.6                        | 0.552                                      | 2.5    | 3.51                                     |
| 310                                                               | 1142.2                         | 1.319                | 0.01438                                     | 0.1259                                  | 78.1                        | 0.518                                      | 2.4    | 4.00                                     |
| 320                                                               | 1097.4                         | 1.391                | 0.01278                                     | 0.1165                                  | 73.4                        | 0.481                                      | 2.4    | 4.69                                     |
| 330                                                               | 1047.5                         | 1.495                | 0.01127                                     | 0.1075                                  | 68.6                        | 0.438                                      | 2.5    | 5.75                                     |
| 340                                                               | 990.1                          | 1.665                | 0.00980                                     | 0.0989                                  | 63.6                        | 0.386                                      | 2.6    | 7.56                                     |
| 350                                                               | 920.1                          | 1.997                | 0.00831                                     | 0.0904                                  | 58.3                        | 0.317                                      | 2.8    | 11.35                                    |
| 360                                                               | 823.4                          | 3.001                | 0.00668                                     | 0.0811                                  | 53.1                        | 0.215                                      | 3.8    | 23.88                                    |
| <b>Mercury (Hg)</b>                                               |                                |                      |                                             |                                         |                             |                                            |        |                                          |
| 273                                                               | 13,595                         | 0.1404               | 0.1688                                      | 0.1240                                  | 8180                        | 42.85                                      | 0.0290 | 0.181                                    |
| 300                                                               | 13,529                         | 0.1393               | 0.1523                                      | 0.1125                                  | 8540                        | 45.30                                      | 0.0248 | 0.181                                    |
| 350                                                               | 13,407                         | 0.1377               | 0.1309                                      | 0.0976                                  | 9180                        | 49.75                                      | 0.0196 | 0.181                                    |
| 400                                                               | 13,287                         | 0.1365               | 0.1171                                      | 0.0882                                  | 9800                        | 54.05                                      | 0.0163 | 0.181                                    |
| 450                                                               | 13,167                         | 0.1357               | 0.1075                                      | 0.0816                                  | 10,400                      | 58.10                                      | 0.0140 | 0.181                                    |
| 500                                                               | 13,048                         | 0.1353               | 0.1007                                      | 0.0771                                  | 10,950                      | 61.90                                      | 0.0125 | 0.182                                    |
| 550                                                               | 12,929                         | 0.1352               | 0.0953                                      | 0.0737                                  | 11,450                      | 65.55                                      | 0.0112 | 0.184                                    |
| 600                                                               | 12,809                         | 0.1355               | 0.0911                                      | 0.0711                                  | 11,950                      | 68.80                                      | 0.0103 | 0.187                                    |

**TABLE A.5** Continued*Saturated Liquid–Vapor, 1 atm<sup>b</sup>*

| Fluid              | $T_{\text{sat}}$<br>(K) | $h_{fg}$<br>(kJ/kg) | $\rho_f$<br>(kg/m <sup>3</sup> ) | $\rho_g$<br>(kg/m <sup>3</sup> ) | $\sigma \cdot 10^3$<br>(N/m) |
|--------------------|-------------------------|---------------------|----------------------------------|----------------------------------|------------------------------|
| Ethanol            | 351                     | 846                 | 757                              | 1.44                             | 17.7                         |
| Ethylene glycol    | 470                     | 812                 | 1111 <sup>c</sup>                | —                                | 32.7                         |
| Glycerin           | 563                     | 974                 | 1260 <sup>c</sup>                | —                                | 63.0 <sup>c</sup>            |
| Mercury            | 630                     | 301                 | 12,740                           | 3.90                             | 417                          |
| Refrigerant R-134a | 247                     | 217                 | 1377                             | 5.26                             | 15.4                         |
| Refrigerant R-22   | 232                     | 234                 | 1409                             | 4.70                             | 18.1                         |

<sup>a</sup>Adapted from References 15–19.<sup>b</sup>Adapted from References 8, 20, and 21.<sup>c</sup>Property value corresponding to 300 K.

TABLE A.6 Thermophysical Properties of Saturated Water<sup>a</sup>

| Temperature,<br><i>T</i> (K) | Pressure,<br><i>p</i> (bars) <sup>b</sup> | Specific Volume<br>(m <sup>3</sup> /kg) |       | Heat of Vaporization,<br><i>h<sub>fg</sub></i> (kJ/kg) | Specific Heat<br>(kJ/kg·K) |           | Viscosity<br>(N·s/m <sup>2</sup> ) |                    | Thermal Conductivity<br>(W/m·K) |                  | Prandtl Number |        | Surface Tension,<br>$\sigma_f \cdot 10^3$ (N/m) | Expansion Coefficient,<br>$\beta_f \cdot 10^6$ (K <sup>-1</sup> ) | Temperature,<br><i>T</i> (K) |
|------------------------------|-------------------------------------------|-----------------------------------------|-------|--------------------------------------------------------|----------------------------|-----------|------------------------------------|--------------------|---------------------------------|------------------|----------------|--------|-------------------------------------------------|-------------------------------------------------------------------|------------------------------|
|                              |                                           | $v_f \cdot 10^3$                        | $v_g$ |                                                        | $c_{p,f}$                  | $c_{p,g}$ | $\mu_f \cdot 10^6$                 | $\mu_g \cdot 10^6$ | $k_f \cdot 10^3$                | $k_g \cdot 10^3$ | $Pr_f$         | $Pr_g$ |                                                 |                                                                   |                              |
| 273.15                       | 0.00611                                   | 1.000                                   | 206.3 | 2502                                                   | 4.217                      | 1.854     | 1750                               | 8.02               | 569                             | 18.2             | 12.99          | 0.815  | 75.5                                            | -68.05                                                            | 273.15                       |
| 275                          | 0.00697                                   | 1.000                                   | 181.7 | 2497                                                   | 4.211                      | 1.855     | 1652                               | 8.09               | 574                             | 18.3             | 12.22          | 0.817  | 75.3                                            | -32.74                                                            | 275                          |
| 280                          | 0.00990                                   | 1.000                                   | 130.4 | 2485                                                   | 4.198                      | 1.858     | 1422                               | 8.29               | 582                             | 18.6             | 10.26          | 0.825  | 74.8                                            | 46.04                                                             | 280                          |
| 285                          | 0.01387                                   | 1.000                                   | 99.4  | 2473                                                   | 4.189                      | 1.861     | 1225                               | 8.49               | 590                             | 18.9             | 8.81           | 0.833  | 74.3                                            | 114.1                                                             | 285                          |
| 290                          | 0.01917                                   | 1.001                                   | 69.7  | 2461                                                   | 4.184                      | 1.864     | 1080                               | 8.69               | 598                             | 19.3             | 7.56           | 0.841  | 73.7                                            | 174.0                                                             | 290                          |
| 295                          | 0.02617                                   | 1.002                                   | 51.94 | 2449                                                   | 4.181                      | 1.868     | 959                                | 8.89               | 606                             | 19.5             | 6.62           | 0.849  | 72.7                                            | 227.5                                                             | 295                          |
| 300                          | 0.03531                                   | 1.003                                   | 39.13 | 2438                                                   | 4.179                      | 1.872     | 855                                | 9.09               | 613                             | 19.6             | 5.83           | 0.857  | 71.7                                            | 276.1                                                             | 300                          |
| 305                          | 0.04712                                   | 1.005                                   | 29.74 | 2426                                                   | 4.178                      | 1.877     | 769                                | 9.29               | 620                             | 20.1             | 5.20           | 0.865  | 70.9                                            | 320.6                                                             | 305                          |
| 310                          | 0.06221                                   | 1.007                                   | 22.93 | 2414                                                   | 4.178                      | 1.882     | 695                                | 9.49               | 628                             | 20.4             | 4.62           | 0.873  | 70.0                                            | 361.9                                                             | 310                          |
| 315                          | 0.08132                                   | 1.009                                   | 17.82 | 2402                                                   | 4.179                      | 1.888     | 631                                | 9.69               | 634                             | 20.7             | 4.16           | 0.883  | 69.2                                            | 400.4                                                             | 315                          |
| 320                          | 0.1053                                    | 1.011                                   | 13.98 | 2390                                                   | 4.180                      | 1.895     | 577                                | 9.89               | 640                             | 21.0             | 3.77           | 0.894  | 68.3                                            | 436.7                                                             | 320                          |
| 325                          | 0.1351                                    | 1.013                                   | 11.06 | 2378                                                   | 4.182                      | 1.903     | 528                                | 10.09              | 645                             | 21.3             | 3.42           | 0.901  | 67.5                                            | 471.2                                                             | 325                          |
| 330                          | 0.1719                                    | 1.016                                   | 8.82  | 2366                                                   | 4.184                      | 1.911     | 489                                | 10.29              | 650                             | 21.7             | 3.15           | 0.908  | 66.6                                            | 504.0                                                             | 330                          |
| 335                          | 0.2167                                    | 1.018                                   | 7.09  | 2354                                                   | 4.186                      | 1.920     | 453                                | 10.49              | 656                             | 22.0             | 2.88           | 0.916  | 65.8                                            | 535.5                                                             | 335                          |
| 340                          | 0.2713                                    | 1.021                                   | 5.74  | 2342                                                   | 4.188                      | 1.930     | 420                                | 10.69              | 660                             | 22.3             | 2.66           | 0.925  | 64.9                                            | 566.0                                                             | 340                          |
| 345                          | 0.3372                                    | 1.024                                   | 4.683 | 2329                                                   | 4.191                      | 1.941     | 389                                | 10.89              | 668                             | 22.6             | 2.45           | 0.933  | 64.1                                            | 595.4                                                             | 345                          |
| 350                          | 0.4163                                    | 1.027                                   | 3.846 | 2317                                                   | 4.195                      | 1.954     | 365                                | 11.09              | 668                             | 23.0             | 2.29           | 0.942  | 63.2                                            | 624.2                                                             | 350                          |
| 355                          | 0.5100                                    | 1.030                                   | 3.180 | 2304                                                   | 4.199                      | 1.968     | 343                                | 11.29              | 671                             | 23.3             | 2.14           | 0.951  | 62.3                                            | 652.3                                                             | 355                          |
| 360                          | 0.6209                                    | 1.034                                   | 2.645 | 2291                                                   | 4.203                      | 1.983     | 324                                | 11.49              | 674                             | 23.7             | 2.02           | 0.960  | 61.4                                            | 697.9                                                             | 360                          |
| 365                          | 0.7514                                    | 1.038                                   | 2.212 | 2278                                                   | 4.209                      | 1.999     | 306                                | 11.69              | 677                             | 24.1             | 1.91           | 0.969  | 60.5                                            | 707.1                                                             | 365                          |
| 370                          | 0.9040                                    | 1.041                                   | 1.861 | 2265                                                   | 4.214                      | 2.017     | 289                                | 11.89              | 679                             | 24.5             | 1.80           | 0.978  | 59.5                                            | 728.7                                                             | 370                          |
| 373.15                       | 1.0133                                    | 1.044                                   | 1.679 | 2257                                                   | 4.217                      | 2.029     | 279                                | 12.02              | 680                             | 24.8             | 1.76           | 0.984  | 58.9                                            | 750.1                                                             | 373.15                       |
| 375                          | 1.0815                                    | 1.045                                   | 1.574 | 2252                                                   | 4.220                      | 2.036     | 274                                | 12.09              | 681                             | 24.9             | 1.70           | 0.987  | 58.6                                            | 761                                                               | 375                          |
| 380                          | 1.2869                                    | 1.049                                   | 1.337 | 2239                                                   | 4.226                      | 2.057     | 260                                | 12.29              | 683                             | 25.4             | 1.61           | 0.999  | 57.6                                            | 788                                                               | 380                          |
| 385                          | 1.5233                                    | 1.053                                   | 1.142 | 2225                                                   | 4.232                      | 2.080     | 248                                | 12.49              | 685                             | 25.8             | 1.53           | 1.004  | 56.6                                            | 814                                                               | 385                          |
| 390                          | 1.794                                     | 1.058                                   | 0.980 | 2212                                                   | 4.239                      | 2.104     | 237                                | 12.69              | 686                             | 26.3             | 1.47           | 1.013  | 55.6                                            | 841                                                               | 390                          |
| 400                          | 2.455                                     | 1.067                                   | 0.731 | 2183                                                   | 4.256                      | 2.158     | 217                                | 13.05              | 688                             | 27.2             | 1.34           | 1.033  | 53.6                                            | 896                                                               | 400                          |
| 410                          | 3.302                                     | 1.077                                   | 0.553 | 2153                                                   | 4.278                      | 2.221     | 200                                | 13.42              | 688                             | 28.2             | 1.24           | 1.054  | 51.5                                            | 952                                                               | 410                          |
| 420                          | 4.370                                     | 1.088                                   | 0.425 | 2123                                                   | 4.302                      | 2.291     | 185                                | 13.79              | 688                             | 29.8             | 1.16           | 1.075  | 49.4                                            | 1010                                                              | 420                          |
| 430                          | 5.699                                     | 1.099                                   | 0.331 | 2091                                                   | 4.331                      | 2.369     | 173                                | 14.14              | 685                             | 30.4             | 1.09           | 1.10   | 47.2                                            |                                                                   | 430                          |

|                    |       |       |        |      |      |      |     |       |     |      |      |      |      |                    |
|--------------------|-------|-------|--------|------|------|------|-----|-------|-----|------|------|------|------|--------------------|
| 440                | 7.333 | 1.110 | 0.261  | 2059 | 4.36 | 2.46 | 162 | 14.50 | 682 | 31.7 | 1.04 | 1.12 | 45.1 | 440                |
| 450                | 9.319 | 1.123 | 0.208  | 2024 | 4.40 | 2.56 | 152 | 14.85 | 678 | 33.1 | 0.99 | 1.14 | 42.9 | 450                |
| 460                | 11.71 | 1.137 | 0.167  | 1989 | 4.44 | 2.68 | 143 | 15.19 | 673 | 34.6 | 0.95 | 1.17 | 40.7 | 460                |
| 470                | 14.55 | 1.152 | 0.136  | 1951 | 4.48 | 2.79 | 136 | 15.54 | 667 | 36.3 | 0.92 | 1.20 | 38.5 | 470                |
| 480                | 17.90 | 1.167 | 0.111  | 1912 | 4.53 | 2.94 | 129 | 15.88 | 660 | 38.1 | 0.89 | 1.23 | 36.2 | 480                |
| 490                | 21.83 | 1.184 | 0.0922 | 1870 | 4.59 | 3.10 | 124 | 16.23 | 651 | 40.1 | 0.87 | 1.25 | 33.9 | 490                |
| 500                | 26.40 | 1.203 | 0.0766 | 1825 | 4.66 | 3.27 | 118 | 16.59 | 642 | 42.3 | 0.86 | 1.28 | 31.6 | 500                |
| 510                | 31.66 | 1.222 | 0.0631 | 1779 | 4.74 | 3.47 | 113 | 16.95 | 631 | 44.7 | 0.85 | 1.31 | 29.3 | 510                |
| 520                | 37.70 | 1.244 | 0.0525 | 1730 | 4.84 | 3.70 | 108 | 17.33 | 621 | 47.5 | 0.84 | 1.35 | 26.9 | 520                |
| 530                | 44.58 | 1.268 | 0.0445 | 1679 | 4.95 | 3.96 | 104 | 17.72 | 608 | 50.6 | 0.85 | 1.39 | 24.5 | 530                |
| 540                | 52.38 | 1.294 | 0.0375 | 1622 | 5.08 | 4.27 | 101 | 18.1  | 594 | 54.0 | 0.86 | 1.43 | 22.1 | 540                |
| 550                | 61.19 | 1.323 | 0.0317 | 1564 | 5.24 | 4.64 | 97  | 18.6  | 580 | 58.3 | 0.87 | 1.47 | 19.7 | 550                |
| 560                | 71.08 | 1.355 | 0.0269 | 1499 | 5.43 | 5.09 | 94  | 19.1  | 563 | 63.7 | 0.90 | 1.52 | 17.3 | 560                |
| 570                | 82.16 | 1.392 | 0.0228 | 1429 | 5.68 | 5.67 | 91  | 19.7  | 548 | 76.7 | 0.94 | 1.59 | 15.0 | 570                |
| 580                | 94.51 | 1.433 | 0.0193 | 1353 | 6.00 | 6.40 | 88  | 20.4  | 528 | 76.7 | 0.99 | 1.68 | 12.8 | 580                |
| 590                | 108.3 | 1.482 | 0.0163 | 1274 | 6.41 | 7.35 | 84  | 21.5  | 513 | 84.1 | 1.05 | 1.84 | 10.5 | 590                |
| 600                | 123.5 | 1.541 | 0.0137 | 1176 | 7.00 | 8.75 | 81  | 22.7  | 497 | 92.9 | 1.14 | 2.15 | 8.4  | 600                |
| 610                | 137.3 | 1.612 | 0.0115 | 1068 | 7.85 | 11.1 | 77  | 24.1  | 467 | 103  | 1.30 | 2.60 | 6.3  | 610                |
| 620                | 159.1 | 1.705 | 0.0094 | 941  | 9.35 | 15.4 | 72  | 25.9  | 444 | 114  | 1.52 | 3.46 | 4.5  | 620                |
| 625                | 169.1 | 1.778 | 0.0085 | 858  | 10.6 | 18.3 | 70  | 27.0  | 430 | 121  | 1.65 | 4.20 | 3.5  | 625                |
| 630                | 179.7 | 1.856 | 0.0075 | 781  | 12.6 | 22.1 | 67  | 28.0  | 412 | 130  | 2.0  | 4.8  | 2.6  | 630                |
| 635                | 190.9 | 1.935 | 0.0066 | 683  | 16.4 | 27.6 | 64  | 30.0  | 392 | 141  | 2.7  | 6.0  | 1.5  | 635                |
| 640                | 202.7 | 2.075 | 0.0057 | 560  | 26   | 42   | 59  | 32.0  | 367 | 155  | 4.2  | 9.6  | 0.8  | 640                |
| 645                | 215.2 | 2.351 | 0.0045 | 361  | 90   | —    | 54  | 37.0  | 331 | 178  | 12   | 26   | 0.1  | 645                |
| 647.3 <sup>c</sup> | 221.2 | 3.170 | 0.0032 | 0    | ∞    | ∞    | 45  | 45.0  | 238 | 238  | ∞    | ∞    | 0.0  | 647.3 <sup>c</sup> |

<sup>a</sup>Adapted from Reference 22.<sup>b</sup>1 bar = 10<sup>5</sup> N/m<sup>2</sup>.<sup>c</sup>Critical temperature.

**TABLE A.7** Thermophysical Properties of Liquid Metals<sup>a</sup>

| Composition            | Melting Point (K) | $T$ (K)       | $\rho$ (kg/m <sup>3</sup> ) | $c_p$ (kJ/kg · K) | $\nu \cdot 10^7$ (m <sup>2</sup> /s) | $k$ (W/m · K) | $\alpha \cdot 10^5$ (m <sup>2</sup> /s) | $Pr$   |
|------------------------|-------------------|---------------|-----------------------------|-------------------|--------------------------------------|---------------|-----------------------------------------|--------|
| Bismuth                | 544               | 589           | 10,011                      | 0.1444            | 1.617                                | 16.4          | 0.138                                   | 0.0142 |
|                        |                   | 811           | 9739                        | 0.1545            | 1.133                                | 15.6          | 1.035                                   | 0.0110 |
|                        |                   | 1033          | 9467                        | 0.1645            | 0.8343                               | 15.6          | 1.001                                   | 0.0083 |
| Lead                   | 600               | 644           | 10,540                      | 0.159             | 2.276                                | 16.1          | 1.084                                   | 0.024  |
|                        |                   | 755           | 10,412                      | 0.155             | 1.849                                | 15.6          | 1.223                                   | 0.017  |
|                        |                   | 977           | 10,140                      | —                 | 1.347                                | 14.9          | —                                       | —      |
| Potassium              | 337               | 422           | 807.3                       | 0.80              | 4.608                                | 45.0          | 6.99                                    | 0.0066 |
|                        |                   | 700           | 741.7                       | 0.75              | 2.397                                | 39.5          | 7.07                                    | 0.0034 |
|                        |                   | 977           | 674.4                       | 0.75              | 1.905                                | 33.1          | 6.55                                    | 0.0029 |
| Sodium                 | 371               | 366           | 929.1                       | 1.38              | 7.516                                | 86.2          | 6.71                                    | 0.011  |
|                        |                   | 644           | 860.2                       | 1.30              | 3.270                                | 72.3          | 6.48                                    | 0.0051 |
|                        |                   | 977           | 778.5                       | 1.26              | 2.285                                | 59.7          | 6.12                                    | 0.0037 |
| NaK,<br>(45%/55%)      | 292               | 366           | 887.4                       | 1.130             | 6.522                                | 25.6          | 2.552                                   | 0.026  |
|                        |                   | 644           | 821.7                       | 1.055             | 2.871                                | 27.5          | 3.17                                    | 0.0091 |
|                        |                   | 977           | 740.1                       | 1.043             | 2.174                                | 28.9          | 3.74                                    | 0.0058 |
| NaK,<br>(22%/78%)      | 262               | 366           | 849.0                       | 0.946             | 5.797                                | 24.4          | 3.05                                    | 0.019  |
|                        |                   | 672           | 775.3                       | 0.879             | 2.666                                | 26.7          | 3.92                                    | 0.0068 |
|                        |                   | 1033          | 690.4                       | 0.883             | 2.118                                | —             | —                                       | —      |
| PbBi,<br>(44.5%/55.5%) | 398               | 422           | 10,524                      | 0.147             | —                                    | 9.05          | 0.586                                   | —      |
|                        |                   | 644           | 10,236                      | 0.147             | 1.496                                | 11.86         | 0.790                                   | 0.189  |
|                        |                   | 922           | 9835                        | —                 | 1.171                                | —             | —                                       | —      |
| Mercury                | 234               | See Table A.5 |                             |                   |                                      |               |                                         |        |

<sup>a</sup>Adapted from Reference 23.

TABLE A.8 Total, Normal ( $n$ ) or Hemispherical ( $h$ ) Emissivity of Selected Surfaces

| Metallic Solids and Their Oxides <sup>e</sup> |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
|-----------------------------------------------|------------------------------------------------------------------------|------|------|------|------|------|------|------|------|------|------|--|
| Description/Composition                       | Emissivity, $\epsilon_n$ or $\epsilon_h$ , at Various Temperatures (K) |      |      |      |      |      |      |      |      |      |      |  |
|                                               | 100                                                                    | 200  | 300  | 400  | 600  | 800  | 1000 | 1200 | 1500 | 2000 | 2500 |  |
| Aluminum                                      |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Highly polished, film                         | ( <i>h</i> )                                                           | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 |      |      |      |      |      |  |
| Foil, bright                                  | ( <i>h</i> )                                                           | 0.06 | 0.06 | 0.07 |      |      |      |      |      |      |      |  |
| Anodized                                      | ( <i>h</i> )                                                           |      |      | 0.82 | 0.76 |      |      |      |      |      |      |  |
| Chromium                                      |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Polished or plated                            | ( <i>n</i> )                                                           | 0.05 | 0.07 | 0.10 | 0.12 | 0.14 |      |      |      |      |      |  |
| Copper                                        |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Highly polished                               | ( <i>h</i> )                                                           |      |      |      |      | 0.04 | 0.04 | 0.04 |      |      |      |  |
| Stably oxidized                               | ( <i>h</i> )                                                           |      |      | 0.03 | 0.03 | 0.50 | 0.58 | 0.80 |      |      |      |  |
| Gold                                          |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Highly polished or film                       | ( <i>h</i> )                                                           | 0.01 | 0.02 | 0.03 | 0.03 | 0.04 | 0.05 | 0.06 |      |      |      |  |
| Foil, bright                                  | ( <i>h</i> )                                                           | 0.06 | 0.07 | 0.07 |      |      |      |      |      |      |      |  |
| Molybdenum                                    |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Polished                                      | ( <i>h</i> )                                                           |      |      |      |      | 0.06 | 0.08 | 0.10 | 0.12 | 0.15 | 0.21 |  |
| Shot-blasted, rough                           | ( <i>h</i> )                                                           |      |      |      |      | 0.25 | 0.28 | 0.31 | 0.35 | 0.42 |      |  |
| Stably oxidized                               | ( <i>h</i> )                                                           |      |      |      |      | 0.80 | 0.82 |      |      |      | 0.26 |  |
| Nickel                                        |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Polished                                      | ( <i>h</i> )                                                           |      |      |      |      | 0.09 | 0.11 | 0.14 | 0.17 |      |      |  |
| Stably oxidized                               | ( <i>h</i> )                                                           |      |      |      |      | 0.40 | 0.49 | 0.57 |      |      |      |  |
| Platinum                                      |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Polished                                      | ( <i>h</i> )                                                           |      |      |      |      |      | 0.10 | 0.13 | 0.15 | 0.18 |      |  |
| Silver                                        |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Polished                                      | ( <i>h</i> )                                                           |      |      | 0.02 | 0.02 | 0.03 | 0.05 | 0.08 |      |      |      |  |
| Stainless steels                              |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Typical, polished                             | ( <i>n</i> )                                                           |      |      | 0.17 | 0.17 | 0.19 | 0.23 | 0.30 |      |      |      |  |
| Typical, cleaned                              | ( <i>n</i> )                                                           |      |      | 0.22 | 0.22 | 0.24 | 0.28 | 0.35 |      |      |      |  |
| Typical, lightly oxidized                     | ( <i>n</i> )                                                           |      |      |      |      |      | 0.33 | 0.40 |      |      |      |  |
| Typical, highly oxidized                      | ( <i>n</i> )                                                           |      |      |      |      |      | 0.67 | 0.70 | 0.76 |      |      |  |
| AISI 347, stably oxidized                     | ( <i>n</i> )                                                           |      |      |      |      | 0.87 | 0.88 | 0.89 | 0.90 |      |      |  |
| Tantalum                                      |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Polished                                      | ( <i>h</i> )                                                           |      |      |      |      |      |      |      | 0.11 | 0.17 | 0.23 |  |
| Tungsten                                      |                                                                        |      |      |      |      |      |      |      |      |      |      |  |
| Polished                                      | ( <i>h</i> )                                                           |      |      |      |      |      |      | 0.10 | 0.13 | 0.18 | 0.25 |  |
|                                               |                                                                        |      |      |      |      |      |      |      |      |      | 0.29 |  |

TABLE A.8 Continued

*Nonmetallic Substances<sup>b</sup>*

| Description/Composition       |     | Temperature<br>(K) | Emissivity<br>$\epsilon$ |
|-------------------------------|-----|--------------------|--------------------------|
| Aluminum oxide                | (n) | 600                | 0.69                     |
|                               |     | 1000               | 0.55                     |
|                               |     | 1500               | 0.41                     |
| Asphalt pavement              | (h) | 300                | 0.85–0.93                |
| Building materials            |     |                    |                          |
| Asbestos sheet                | (h) | 300                | 0.93–0.96                |
| Brick, red                    | (h) | 300                | 0.93–0.96                |
| Gypsum or plaster board       | (h) | 300                | 0.90–0.92                |
| Wood                          | (h) | 300                | 0.82–0.92                |
| Cloth                         | (h) | 300                | 0.75–0.90                |
| Concrete                      | (h) | 300                | 0.88–0.93                |
| Glass, window                 | (h) | 300                | 0.90–0.95                |
| Ice                           | (h) | 273                | 0.95–0.98                |
| Paints                        |     |                    |                          |
| Black (Parsons)               | (h) | 300                | 0.98                     |
| White, acrylic                | (h) | 300                | 0.90                     |
| White, zinc oxide             | (h) | 300                | 0.92                     |
| Paper, white                  | (h) | 300                | 0.92–0.97                |
| Pyrex                         | (n) | 300                | 0.82                     |
|                               |     | 600                | 0.80                     |
|                               |     | 1000               | 0.71                     |
|                               |     | 1200               | 0.62                     |
| Pyroceram                     | (n) | 300                | 0.85                     |
|                               |     | 600                | 0.78                     |
|                               |     | 1000               | 0.69                     |
|                               |     | 1500               | 0.57                     |
| Refractories (furnace liners) |     |                    |                          |
| Alumina brick                 | (n) | 800                | 0.40                     |
|                               |     | 1000               | 0.33                     |
|                               |     | 1400               | 0.28                     |
|                               |     | 1600               | 0.33                     |
| Magnesia brick                | (n) | 800                | 0.45                     |
|                               |     | 1000               | 0.36                     |
|                               |     | 1400               | 0.31                     |
|                               |     | 1600               | 0.40                     |
| Kaolin insulating brick       | (n) | 800                | 0.70                     |
|                               |     | 1200               | 0.57                     |
|                               |     | 1400               | 0.47                     |
|                               |     | 1600               | 0.53                     |
| Sand                          | (h) | 300                | 0.90                     |
| Silicon carbide               | (n) | 600                | 0.87                     |
|                               |     | 1000               | 0.87                     |
|                               |     | 1500               | 0.85                     |
| Skin                          | (h) | 300                | 0.95                     |
| Snow                          | (h) | 273                | 0.82–0.90                |

TABLE A.8 Continued

Nonmetallic Substances<sup>b</sup>

| Description/Composition |     | Temperature<br>(K) | Emissivity<br>$\epsilon$ |
|-------------------------|-----|--------------------|--------------------------|
| Soil                    | (h) | 300                | 0.93–0.96                |
| Rocks                   | (h) | 300                | 0.88–0.95                |
| Teflon                  | (h) | 300                | 0.85                     |
|                         |     | 400                | 0.87                     |
|                         |     | 500                | 0.92                     |
| Vegetation              | (h) | 300                | 0.92–0.96                |
| Water                   | (h) | 300                | 0.96                     |

<sup>a</sup>Adapted from Reference 1.<sup>b</sup>Adapted from References 1, 9, 24, and 25.TABLE A.9 Solar Radiative Properties for Selected Materials<sup>a</sup>

| Description/Composition     | $\alpha_s$ | $\epsilon^b$ | $\alpha_s/\epsilon$ | $\tau_s$ |
|-----------------------------|------------|--------------|---------------------|----------|
| Aluminum                    |            |              |                     |          |
| Polished                    | 0.09       | 0.03         | 3.0                 |          |
| Anodized                    | 0.14       | 0.84         | 0.17                |          |
| Quartz overcoated           | 0.11       | 0.37         | 0.30                |          |
| Foil                        | 0.15       | 0.05         | 3.0                 |          |
| Brick, red (Purdue)         | 0.63       | 0.93         | 0.68                |          |
| Concrete                    | 0.60       | 0.88         | 0.68                |          |
| Galvanized sheet metal      |            |              |                     |          |
| Clean, new                  | 0.65       | 0.13         | 5.0                 |          |
| Oxidized, weathered         | 0.80       | 0.28         | 2.9                 |          |
| Glass, 3.2-mm thickness     |            |              |                     |          |
| Float or tempered           |            |              |                     | 0.79     |
| Low iron oxide type         |            |              |                     | 0.88     |
| Metal, plated               |            |              |                     |          |
| Black sulfide               | 0.92       | 0.10         | 9.2                 |          |
| Black cobalt oxide          | 0.93       | 0.30         | 3.1                 |          |
| Black nickel oxide          | 0.92       | 0.08         | 11                  |          |
| Black chrome                | 0.87       | 0.09         | 9.7                 |          |
| Mylar, 0.13-mm thickness    |            |              |                     | 0.87     |
| Paints                      |            |              |                     |          |
| Black (Parsons)             | 0.98       | 0.98         | 1.0                 |          |
| White, acrylic              | 0.26       | 0.90         | 0.29                |          |
| White, zinc oxide           | 0.16       | 0.93         | 0.17                |          |
| Plexiglas, 3.2-mm thickness |            |              |                     | 0.90     |
| Snow                        |            |              |                     |          |
| Fine particles, fresh       | 0.13       | 0.82         | 0.16                |          |
| Ice granules                | 0.33       | 0.89         | 0.37                |          |
| Tedlar, 0.10-mm thickness   |            |              |                     | 0.92     |
| Teflon, 0.13-mm thickness   |            |              |                     | 0.92     |

<sup>a</sup>Adapted with permission from Reference 25.<sup>b</sup>The emissivity values in this table correspond to a surface temperature of approximately 300 K.

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# APPENDIX **B**

## *Mathematical Relations and Functions*

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**B.1****Hyperbolic Functions<sup>1</sup>**

| $x$  | $\sinh x$ | $\cosh x$ | $\tanh x$ | $x$    | $\sinh x$ | $\cosh x$ | $\tanh x$ |
|------|-----------|-----------|-----------|--------|-----------|-----------|-----------|
| 0.00 | 0.0000    | 1.0000    | 0.00000   | 2.00   | 3.6269    | 3.7622    | 0.96403   |
| 0.10 | 0.1002    | 1.0050    | 0.09967   | 2.10   | 4.0219    | 4.1443    | 0.97045   |
| 0.20 | 0.2013    | 1.0201    | 0.19738   | 2.20   | 4.4571    | 4.5679    | 0.97574   |
| 0.30 | 0.3045    | 1.0453    | 0.29131   | 2.30   | 4.9370    | 5.0372    | 0.98010   |
| 0.40 | 0.4108    | 1.0811    | 0.37995   | 2.40   | 5.4662    | 5.5569    | 0.98367   |
| 0.50 | 0.5211    | 1.1276    | 0.46212   | 2.50   | 6.0502    | 6.1323    | 0.98661   |
| 0.60 | 0.6367    | 1.1855    | 0.53705   | 2.60   | 6.6947    | 6.7690    | 0.98903   |
| 0.70 | 0.7586    | 1.2552    | 0.60437   | 2.70   | 7.4063    | 7.4735    | 0.99101   |
| 0.80 | 0.8881    | 1.3374    | 0.66404   | 2.80   | 8.1919    | 8.2527    | 0.99263   |
| 0.90 | 1.0265    | 1.4331    | 0.71630   | 2.90   | 9.0596    | 9.1146    | 0.99396   |
| 1.00 | 1.1752    | 1.5431    | 0.76159   | 3.00   | 10.018    | 10.068    | 0.99505   |
| 1.10 | 1.3356    | 1.6685    | 0.80050   | 3.50   | 16.543    | 16.573    | 0.99818   |
| 1.20 | 1.5095    | 1.8107    | 0.83365   | 4.00   | 27.290    | 27.308    | 0.99933   |
| 1.30 | 1.6984    | 1.9709    | 0.86172   | 4.50   | 45.003    | 45.014    | 0.99975   |
| 1.40 | 1.9043    | 2.1509    | 0.88535   | 5.00   | 74.203    | 74.210    | 0.99991   |
| 1.50 | 2.1293    | 2.3524    | 0.90515   | 6.00   | 201.71    | 201.72    | 0.99999   |
| 1.60 | 2.3756    | 2.5775    | 0.92167   | 7.00   | 548.32    | 548.32    | 1.0000    |
| 1.70 | 2.6456    | 2.8283    | 0.93541   | 8.00   | 1490.5    | 1490.5    | 1.0000    |
| 1.80 | 2.9422    | 3.1075    | 0.94681   | 9.00   | 4051.5    | 4051.5    | 1.0000    |
| 1.90 | 3.2682    | 3.4177    | 0.95624   | 10.000 | 11013     | 11013     | 1.0000    |

<sup>1</sup>The hyperbolic functions are defined as

$$\sinh x = \frac{1}{2}(e^x - e^{-x}) \quad \cosh x = \frac{1}{2}(e^x + e^{-x}) \quad \tanh x = \frac{e^x - e^{-x}}{e^x + e^{-x}} = \frac{\sinh x}{\cosh x}$$

The derivatives of the hyperbolic functions of the variable  $u$  are given as

$$\frac{d}{dx}(\sinh u) = (\cosh u) \frac{du}{dx} \quad \frac{d}{dx}(\cosh u) = (\sinh u) \frac{du}{dx} \quad \frac{d}{dx}(\tanh u) = \left( \frac{1}{\cosh^2 u} \right) \frac{du}{dx}$$

**B.2****Gaussian Error Function<sup>1</sup>**

| $w$  | $\text{erf } w$ | $w$  | $\text{erf } w$ | $w$  | $\text{erf } w$ |
|------|-----------------|------|-----------------|------|-----------------|
| 0.00 | 0.00000         | 0.36 | 0.38933         | 1.04 | 0.85865         |
| 0.02 | 0.02256         | 0.38 | 0.40901         | 1.08 | 0.87333         |
| 0.04 | 0.04511         | 0.40 | 0.42839         | 1.12 | 0.88679         |
| 0.06 | 0.06762         | 0.44 | 0.46622         | 1.16 | 0.89910         |
| 0.08 | 0.09008         | 0.48 | 0.50275         | 1.20 | 0.91031         |
| 0.10 | 0.11246         | 0.52 | 0.53790         | 1.30 | 0.93401         |
| 0.12 | 0.13476         | 0.56 | 0.57162         | 1.40 | 0.95228         |
| 0.14 | 0.15695         | 0.60 | 0.60386         | 1.50 | 0.96611         |
| 0.16 | 0.17901         | 0.64 | 0.63459         | 1.60 | 0.97635         |
| 0.18 | 0.20094         | 0.68 | 0.66378         | 1.70 | 0.98379         |
| 0.20 | 0.22270         | 0.72 | 0.69143         | 1.80 | 0.98909         |
| 0.22 | 0.24430         | 0.76 | 0.71754         | 1.90 | 0.99279         |
| 0.24 | 0.26570         | 0.80 | 0.74210         | 2.00 | 0.99532         |
| 0.26 | 0.28690         | 0.84 | 0.76514         | 2.20 | 0.99814         |
| 0.28 | 0.30788         | 0.88 | 0.78669         | 2.40 | 0.99931         |
| 0.30 | 0.32863         | 0.92 | 0.80677         | 2.60 | 0.99976         |
| 0.32 | 0.34913         | 0.96 | 0.82542         | 2.80 | 0.99992         |
| 0.34 | 0.36936         | 1.00 | 0.84270         | 3.00 | 0.99998         |

<sup>1</sup>The Gaussian error function is defined as

$$\text{erf } w = \frac{2}{\sqrt{\pi}} \int_0^w e^{-v^2} dv$$

The complementary error function is defined as

$$\text{erfc } w \equiv 1 - \text{erf } w$$

**B.3**

*The First Four Roots of the Transcendental Equation,  $\xi_n \tan \xi_n = Bi$ , for Transient Conduction in a Plane Wall*

| $Bi = \frac{hL}{k}$ | $\xi_1$ | $\xi_2$ | $\xi_3$ | $\xi_4$ |
|---------------------|---------|---------|---------|---------|
| 0                   | 0       | 3.1416  | 6.2832  | 9.4248  |
| 0.001               | 0.0316  | 3.1419  | 6.2833  | 9.4249  |
| 0.002               | 0.0447  | 3.1422  | 6.2835  | 9.4250  |
| 0.004               | 0.0632  | 3.1429  | 6.2838  | 9.4252  |
| 0.006               | 0.0774  | 3.1435  | 6.2841  | 9.4254  |
| 0.008               | 0.0893  | 3.1441  | 6.2845  | 9.4256  |
| 0.01                | 0.0998  | 3.1448  | 6.2848  | 9.4258  |
| 0.02                | 0.1410  | 3.1479  | 6.2864  | 9.4269  |
| 0.04                | 0.1987  | 3.1543  | 6.2895  | 9.4290  |
| 0.06                | 0.2425  | 3.1606  | 6.2927  | 9.4311  |
| 0.08                | 0.2791  | 3.1668  | 6.2959  | 9.4333  |
| 0.1                 | 0.3111  | 3.1731  | 6.2991  | 9.4354  |
| 0.2                 | 0.4328  | 3.2039  | 6.3148  | 9.4459  |
| 0.3                 | 0.5218  | 3.2341  | 6.3305  | 9.4565  |
| 0.4                 | 0.5932  | 3.2636  | 6.3461  | 9.4670  |
| 0.5                 | 0.6533  | 3.2923  | 6.3616  | 9.4775  |
| 0.6                 | 0.7051  | 3.3204  | 6.3770  | 9.4879  |
| 0.7                 | 0.7506  | 3.3477  | 6.3923  | 9.4983  |
| 0.8                 | 0.7910  | 3.3744  | 6.4074  | 9.5087  |
| 0.9                 | 0.8274  | 3.4003  | 6.4224  | 9.5190  |
| 1.0                 | 0.8603  | 3.4256  | 6.4373  | 9.5293  |
| 1.5                 | 0.9882  | 3.5422  | 6.5097  | 9.5801  |
| 2.0                 | 1.0769  | 3.6436  | 6.5783  | 9.6296  |
| 3.0                 | 1.1925  | 3.8088  | 6.7040  | 9.7240  |
| 4.0                 | 1.2646  | 3.9352  | 6.8140  | 9.8119  |
| 5.0                 | 1.3138  | 4.0336  | 6.9096  | 9.8928  |
| 6.0                 | 1.3496  | 4.1116  | 6.9924  | 9.9667  |
| 7.0                 | 1.3766  | 4.1746  | 7.0640  | 10.0339 |
| 8.0                 | 1.3978  | 4.2264  | 7.1263  | 10.0949 |
| 9.0                 | 1.4149  | 4.2694  | 7.1806  | 10.1502 |
| 10.0                | 1.4289  | 4.3058  | 7.2281  | 10.2003 |
| 15.0                | 1.4729  | 4.4255  | 7.3959  | 10.3898 |
| 20.0                | 1.4961  | 4.4915  | 7.4954  | 10.5117 |
| 30.0                | 1.5202  | 4.5615  | 7.6057  | 10.6543 |
| 40.0                | 1.5325  | 4.5979  | 7.6647  | 10.7334 |
| 50.0                | 1.5400  | 4.6202  | 7.7012  | 10.7832 |
| 60.0                | 1.5451  | 4.6353  | 7.7259  | 10.8172 |
| 80.0                | 1.5514  | 4.6543  | 7.7573  | 10.8606 |
| 100.0               | 1.5552  | 4.6658  | 7.7764  | 10.8871 |
| $\infty$            | 1.5708  | 4.7124  | 7.8540  | 10.9956 |

**B.4*****Bessel Functions of the First Kind***


---

| $x$ | $J_0(x)$ | $J_1(x)$ |
|-----|----------|----------|
| 0.0 | 1.0000   | 0.0000   |
| 0.1 | 0.9975   | 0.0499   |
| 0.2 | 0.9900   | 0.0995   |
| 0.3 | 0.9776   | 0.1483   |
| 0.4 | 0.9604   | 0.1960   |
| 0.5 | 0.9385   | 0.2423   |
| 0.6 | 0.9120   | 0.2867   |
| 0.7 | 0.8812   | 0.3290   |
| 0.8 | 0.8463   | 0.3688   |
| 0.9 | 0.8075   | 0.4059   |
| 1.0 | 0.7652   | 0.4400   |
| 1.1 | 0.7196   | 0.4709   |
| 1.2 | 0.6711   | 0.4983   |
| 1.3 | 0.6201   | 0.5220   |
| 1.4 | 0.5669   | 0.5419   |
| 1.5 | 0.5118   | 0.5579   |
| 1.6 | 0.4554   | 0.5699   |
| 1.7 | 0.3980   | 0.5778   |
| 1.8 | 0.3400   | 0.5815   |
| 1.9 | 0.2818   | 0.5812   |
| 2.0 | 0.2239   | 0.5767   |
| 2.1 | 0.1666   | 0.5683   |
| 2.2 | 0.1104   | 0.5560   |
| 2.3 | 0.0555   | 0.5399   |
| 2.4 | 0.0025   | 0.5202   |

---

**B.5****Modified Bessel Functions<sup>1</sup> of  
the First and Second Kinds**

| $x$  | $e^{-x}I_0(x)$ | $e^{-x}I_1(x)$ | $e^xK_0(x)$ | $e^xK_1(x)$ |
|------|----------------|----------------|-------------|-------------|
| 0.0  | 1.0000         | 0.0000         | $\infty$    | $\infty$    |
| 0.2  | 0.8269         | 0.0823         | 2.1407      | 5.8334      |
| 0.4  | 0.6974         | 0.1368         | 1.6627      | 3.2587      |
| 0.6  | 0.5993         | 0.1722         | 1.4167      | 2.3739      |
| 0.8  | 0.5241         | 0.1945         | 1.2582      | 1.9179      |
| 1.0  | 0.4657         | 0.2079         | 1.1445      | 1.6361      |
| 1.2  | 0.4198         | 0.2152         | 1.0575      | 1.4429      |
| 1.4  | 0.3831         | 0.2185         | 0.9881      | 1.3010      |
| 1.6  | 0.3533         | 0.2190         | 0.9309      | 1.1919      |
| 1.8  | 0.3289         | 0.2177         | 0.8828      | 1.1048      |
| 2.0  | 0.3085         | 0.2153         | 0.8416      | 1.0335      |
| 2.2  | 0.2913         | 0.2121         | 0.8056      | 0.9738      |
| 2.4  | 0.2766         | 0.2085         | 0.7740      | 0.9229      |
| 2.6  | 0.2639         | 0.2046         | 0.7459      | 0.8790      |
| 2.8  | 0.2528         | 0.2007         | 0.7206      | 0.8405      |
| 3.0  | 0.2430         | 0.1968         | 0.6978      | 0.8066      |
| 3.2  | 0.2343         | 0.1930         | 0.6770      | 0.7763      |
| 3.4  | 0.2264         | 0.1892         | 0.6579      | 0.7491      |
| 3.6  | 0.2193         | 0.1856         | 0.6404      | 0.7245      |
| 3.8  | 0.2129         | 0.1821         | 0.6243      | 0.7021      |
| 4.0  | 0.2070         | 0.1787         | 0.6093      | 0.6816      |
| 4.2  | 0.2016         | 0.1755         | 0.5953      | 0.6627      |
| 4.4  | 0.1966         | 0.1724         | 0.5823      | 0.6453      |
| 4.6  | 0.1919         | 0.1695         | 0.5701      | 0.6292      |
| 4.8  | 0.1876         | 0.1667         | 0.5586      | 0.6142      |
| 5.0  | 0.1835         | 0.1640         | 0.5478      | 0.6003      |
| 5.2  | 0.1797         | 0.1614         | 0.5376      | 0.5872      |
| 5.4  | 0.1762         | 0.1589         | 0.5279      | 0.5749      |
| 5.6  | 0.1728         | 0.1565         | 0.5188      | 0.5633      |
| 5.8  | 0.1696         | 0.1542         | 0.5101      | 0.5525      |
| 6.0  | 0.1666         | 0.1520         | 0.5019      | 0.5422      |
| 6.4  | 0.1611         | 0.1479         | 0.4865      | 0.5232      |
| 6.8  | 0.1561         | 0.1441         | 0.4724      | 0.5060      |
| 7.2  | 0.1515         | 0.1405         | 0.4595      | 0.4905      |
| 7.6  | 0.1473         | 0.1372         | 0.4476      | 0.4762      |
| 8.0  | 0.1434         | 0.1341         | 0.4366      | 0.4631      |
| 8.4  | 0.1398         | 0.1312         | 0.4264      | 0.4511      |
| 8.8  | 0.1365         | 0.1285         | 0.4168      | 0.4399      |
| 9.2  | 0.1334         | 0.1260         | 0.4079      | 0.4295      |
| 9.6  | 0.1305         | 0.1235         | 0.3995      | 0.4198      |
| 10.0 | 0.1278         | 0.1213         | 0.3916      | 0.4108      |

<sup>1</sup> $I_{n+1}(x) = I_{n-1}(x) - (2n/x)I_n(x)$